

## ARTICLE 24

# More Evidence for the '120 Polyhedron' As the 3-dimensional Realisation of the Inner Tree of Life and Its Manifestation in the $E_8 \times E_8$ Heterotic Superstring

by

Stephen M. Phillips

Flat 3, 32 Surrey Road South. Bournemouth. Dorset BH4 9BP. England.

E-mail: [stephen@smphillips.8m.com](mailto:stephen@smphillips.8m.com)  
Website: <http://www.smphillips.8m.com>

## Abstract

Article 22 presented evidence that the **120 Polyhedron** represents the 3-dimensional manifestation of the exterior aspect of the 2-dimensional, inner form of the Tree of Life — the geometrical representation of "Adam Kadmon," or Divine Man. Its 62 vertices define 28 regular and semi-regular solids. Constructed from Pythagorean tetractyses, the template of sacred geometry, they are made up of 3360 hexagonal yods. This number is the number of yods in the seven enfolded, regular polygons forming half of the inner Tree of Life. This is further confirmation that the **120 Polyhedron** is the 3-dimensional realisation of the inner Tree of Life. Its manifestation in superstring space-time are the 3360 circularly polarised oscillations made during one complete revolution by the ten component closed curves of the  $E_8 \times E_8$  heterotic superstring, as described 109 years ago by the Theosophists Annie Besant and C.W. Leadbeater.

## 1. Introduction

Articles 22 and 23 showed that the so-called '120 Polyhedron' and the '144 Polyhedron' that were part of the 'Pattern' observed by Lynnclaire Dennis during her NDE<sup>1</sup> in 1987 represent the exterior and the interior of what the author calls the 'inner form of the Tree of Life.' Through the equivalence between the  $(6n+1)$  yods of an  $n$ -sided regular polygon with its sectors turned into tetractyses and the  $(6n+1)$  Sephirothic emanations up to Chesed of the highest tree in  $n$  overlapping Trees of Life, this inner form can be shown<sup>2</sup> to encode the replication of its outer form to map all levels of reality, both physical space-time and superphysical realms. The seven enfolded, regular polygons

1432 (p. 1)  
PHILLIPS, S.M.  
2004 22.

## ARTICLE 24

# **More Evidence for the Disdyakis Triacontahedron as the 3-dimensional Realisation of the Inner Tree of Life & Its Manifestation in the $E_8 \times E_8$ Heterotic Superstring**

by

**Stephen M. Phillips**

Flat 3, 32 Surrey Road South. Bournemouth. Dorset BH4 9BP. England.

E-mail: [stephen@smphillips.8m.com](mailto:stephen@smphillips.8m.com)  
Website: <http://www.smphillips.8m.com>

### **Abstract**

*Article 22 presented evidence that the disdyakis triacontahedron represents the 3-dimensional manifestation of the exterior aspect of the 2-dimensional, inner form of the Tree of Life — the geometrical representation of “Adam Kadmon,” or Divine Man. Its 62 vertices define 28 regular and semi-regular solids. Constructed from Pythagorean tetractyses, the template of sacred geometry, they are made up of 3360 hexagonal yods. This number is the number of yods in the seven enfolded, regular polygons forming half of the inner Tree of Life. It is further confirmation that the disdyakis triacontahedron is the 3-dimensional realisation of the inner Tree of Life. Its manifestation in superstring space-time are the 3360 circularly polarised oscillations made during one complete revolution by the ten component closed curves of the  $E_8 \times E_8$  heterotic superstring, as described 114 years ago by the Theosophists Annie Besant and C.W. Leadbeater.*

### **1. Introduction**

The author has discovered that what is known to Kabbalists as the ‘Tree of Life’ is actually only the outer form of the complete, sacred geometrical system embodying the divine paradigm. It has an inner form, and Articles 22 and 23 showed that the Catalan solid called the ‘disdyakis triacontahedron’ is its polyhedral manifestation. Through the equivalence between the  $(6n+1)$  yods of an  $n$ -sided, regular polygon with its sectors turned into tetractyses and the  $(6n+1)$  Sephirothic emanations up to Chesed of the highest tree in  $n$  overlapping Trees of Life, this inner form can be shown<sup>1</sup> to encode the replication of its outer form to map all levels of reality, both physical space-time and

Table 1. Gematria number values of the ten Sephiroth in the four Worlds.

|    | SEPHIRAH                              | GODNAME                                                       | ARCHANGEL                                         | ORDER OF ANGELS                                            | MUNDANE CHAKRA                                                                                  |
|----|---------------------------------------|---------------------------------------------------------------|---------------------------------------------------|------------------------------------------------------------|-------------------------------------------------------------------------------------------------|
| 1  | Kether<br>(Crown)<br><b>620</b>       | EHYEH<br>(I am)<br><b>21</b>                                  | Metatron<br>(Angel of the Presence)<br><b>314</b> | Chaioth ha Qadesh<br>(Holy Living Creatures)<br><b>833</b> | Rashith ha Gilgalim<br>First Swirlings.<br>(Primum Mobile)<br><b>636</b>                        |
| 2  | Chokmah<br>(Wisdom)<br><b>73</b>      | YAHVEH, YAH<br>(The Lord)<br><b>26, 15</b>                    | Raziel<br>(Herald of the Deity)<br><b>248</b>     | Auphanim<br>(Wheels)<br><b>187</b>                         | Masloth<br>(The Sphere of the Zodiac)<br><b>140</b>                                             |
| 3  | Binah<br>(Understanding)<br><b>67</b> | ELOHIM<br>(God in multiplicity)<br><b>50</b>                  | Tzaphkiel<br>(Contemplation of God)<br><b>311</b> | Aralim<br>(Thrones)<br><b>282</b>                          | Shabathai<br>Rest.<br>(Saturn)<br><b>317</b>                                                    |
|    | Daath<br>(Knowledge)<br><b>474</b>    |                                                               |                                                   |                                                            |                                                                                                 |
| 4  | Chesed<br>(Mercy)<br><b>72</b>        | EL<br>(God)<br><b>31</b>                                      | Tzadkiel<br>(Benevolence of God)<br><b>62</b>     | Chasmalim<br>(Shining Ones)<br><b>428</b>                  | Tzadekh<br>Righteousness.<br>(Jupiter)<br><b>194</b>                                            |
| 5  | Geburah<br>(Severity)<br><b>216</b>   | ELOHA<br>(The Almighty)<br><b>36</b>                          | Samael<br>(Severity of God)<br><b>131</b>         | Seraphim<br>(Fiery Serpents)<br><b>630</b>                 | Madim<br>Vehement Strength.<br>(Mars)<br><b>95</b>                                              |
| 6  | Tiphareth<br>(Beauty)<br><b>1081</b>  | YAHVEH<br>ELOHIM<br>(God the Creator)<br><b>76</b>            | Michael<br>(Like unto God)<br><b>101</b>          | Malachim<br>(Kings)<br><b>140</b>                          | Shemesh<br>The Solar Light.<br>(Sun)<br><b>640</b>                                              |
| 7  | Netzach<br>(Victory)<br><b>148</b>    | YAHVEH<br>SABAOOTH<br>(Lord of Hosts)<br><b>129</b>           | Haniel<br>(Grace of God)<br><b>97</b>             | Tarshishim or Elohim<br><b>1260</b>                        | Nogah<br>Glittering Splendour.<br>(Venus)<br><b>64</b>                                          |
| 8  | Hod<br>(Glory)<br><b>15</b>           | ELOHIM<br>SABAOOTH<br>(God of Hosts)<br><b>153</b>            | Raphael<br>(Divine Physician)<br><b>311</b>       | Beni Elohim<br>(Sons of God)<br><b>112</b>                 | Kokab<br>The Stellar Light.<br>(Mercury)<br><b>48</b>                                           |
| 9  | Yesod<br>(Foundation)<br><b>80</b>    | SHADDAI EL<br>CHAI<br>(Almighty Living God)<br><b>49, 363</b> | Gabriel<br>(Strong Man of God)<br><b>246</b>      | Cherubim<br>(The Strong)<br><b>272</b>                     | Levanah<br>The Lunar Flame.<br>(Moon)<br><b>87</b>                                              |
| 10 | Malkuth<br>(Kingdom)<br><b>496</b>    | ADONAI<br>MELEKH<br>(The Lord and King)<br><b>65, 155</b>     | Sandalphon<br>(Manifest Messiah)<br><b>280</b>    | Ashim<br>(Souls of Fire)<br><b>351</b>                     | Cholem<br>Yesodeth<br>The Breaker of the Foundations.<br>The Elements.<br>(Earth)<br><b>168</b> |

*The Sephiroth exist in the four Worlds of Atziluth, Beriah, Yetzirah and Assiyah. Corresponding to them are the Godnames, Archangels, Order of Angels and Mundane Chakras (their physical manifestation). This table gives their number values obtained by the ancient practice of gematria, wherein a number is assigned to each letter of the alphabet, thereby giving a number value to a word that is the sum of the numbers of its letters.*

(All numbers from this table that are referred to in the article are written in **boldface**).

superphysical realms. The seven enfolded, regular polygons constituting one half of the inner Tree of Life map what are known in Theosophy as the **49** subplanes of the seven planes of consciousness: physical, astral, mental, buddhic, atmic, anupadaka (or Monadic) and adi (or Divine), each subplane being represented by its own Tree of Life.

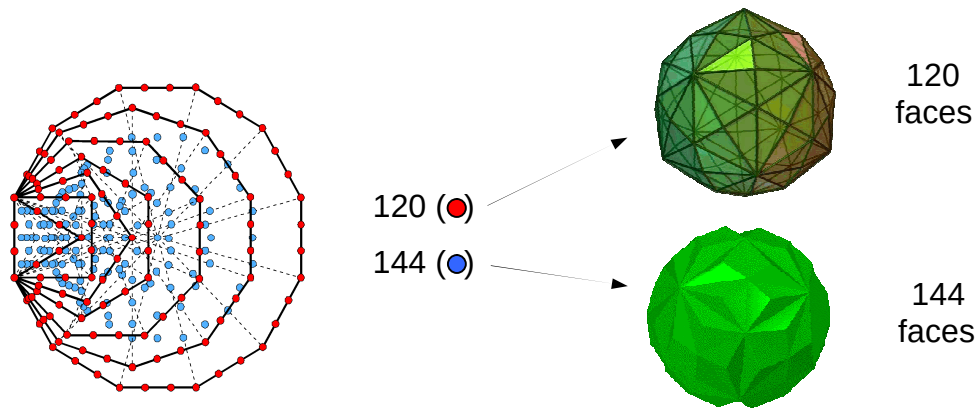


Figure 1. The 120 yods on the boundaries of the seven enfolded polygons symbolise the 120 faces of the disdyakis triacontahedron and the 144 internal yods of the inner Tree of Life symbolise the 144 faces of a polyhedron with 74 vertices.

The 120 yods on the boundaries of the seven polygons signify the 120 faces of the disdyakis triacontahedron and the 144 yods inside them denote the 144 faces of another polyhedron (Fig. 1). This '144 Polyhedron' was identified in Article 23 as generated from the disdyakis dodecahedron (one of the 13 Catalan solids), which has **48** faces, **26** vertices & **72** edges. This is the only semi-regular polyhedron that has **48** faces, which means that it, alone, can generate a polyhedron with 144 faces when tetrahedra are stuck on its faces.

## 2. Polyhedral content of the disdyakis triacontahedron

The **62** vertices of the disdyakis triacontahedron define the vertices of 28 regular and semi-regular solids: ten tetrahedra, five cubes, five octahedra, one icosahedron, one dodecahedron, five rhombic dodecahedra and one rhombic triacontahedron. A rhombic dodecahedron (Fig. 2) is an Archimedean solid with 14 vertices, 24 edges and 12 rhombic faces. Constructed from four tetractyses, each of the 12 rhombic faces has 12 internal hexagonal yods, whilst two hexagonal yods lie on each of its 24 edges. The number of hexagonal yods in the rhombic dodecahedron is therefore  $2 \times 24 + 12 \times 12 =$

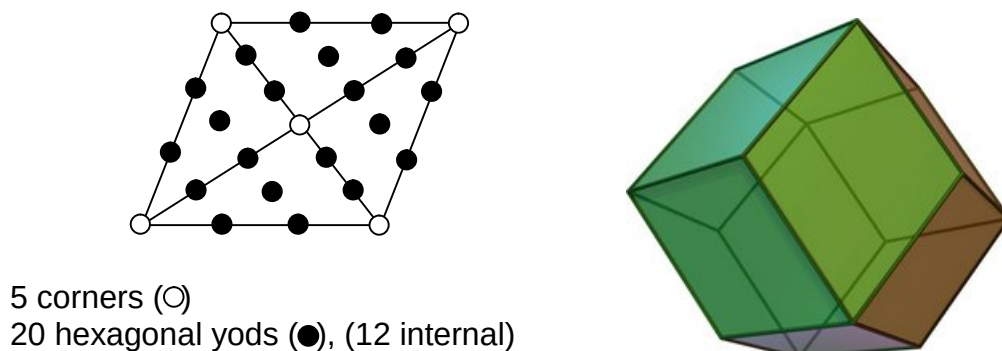


Figure 2. The 12 faces of the rhombic dodecahedron contain **48** hexagonal yods on its 24 edges and 144 internal hexagonal yods.

192 (see Article 18 for the significance of this parameter of holistic systems vis-à-vis the I Ching table and the Bode numbers of the planets). When the five, separate rhombic dodecahedra group, their (5×14=70) separate vertices become the **62** vertices and raised centres of the 30 Golden Rhombic faces of the disdyakis triacontahedron, their 30 unshared vertices coinciding with the centres of these faces and their 32 shared

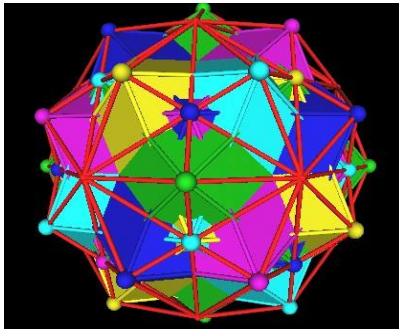


Figure 3. The 30 unshared vertices of the five rhombic dodecahedra coincide with the apices of the pyramids with the golden rhombic faces as bases (shown as coloured balls), leaving their shared vertices at the 32 vertices of these faces, two per vertex (shown as a pair of intersecting coloured lines).

vertices coinciding with their vertices (Fig. 3). Each rhombic dodecahedron has six unshared vertices and eight shared vertices that are vertices of these faces. Each face vertex coincides with two vertices of different dodecahedra:

|                               |                               |                               |                               |
|-------------------------------|-------------------------------|-------------------------------|-------------------------------|
| A <sub>1</sub> B <sub>1</sub> | B <sub>3</sub> C <sub>3</sub> | C <sub>5</sub> D <sub>5</sub> | D <sub>7</sub> E <sub>7</sub> |
| A <sub>2</sub> C <sub>1</sub> | B <sub>4</sub> D <sub>3</sub> | C <sub>6</sub> E <sub>5</sub> | D <sub>8</sub> E <sub>8</sub> |
| A <sub>3</sub> D <sub>1</sub> | B <sub>5</sub> E <sub>3</sub> | C <sub>7</sub> D <sub>6</sub> |                               |
| A <sub>4</sub> E <sub>1</sub> | B <sub>6</sub> C <sub>4</sub> | C <sub>8</sub> E <sub>6</sub> |                               |
| A <sub>5</sub> B <sub>2</sub> | B <sub>7</sub> D <sub>4</sub> |                               |                               |
| A <sub>6</sub> C <sub>2</sub> | B <sub>8</sub> E <sub>4</sub> |                               |                               |
| A <sub>7</sub> D <sub>2</sub> |                               |                               |                               |
| A <sub>8</sub> E <sub>2</sub> |                               |                               |                               |

where the letters label the five dodecahedra and the numbers indicate their vertices.

Let us now construct the 28 solids from tetractyses — the template of sacred geometry — and then work out their populations of hexagonal yods. The significance of the latter is that the seven hexagonal yods of the tetractys symbolise the seven Sephiroth of Construction, the formative degrees of freedom expressing the 'objective' aspects of God). The hexagonal yod populations of the 28 solids in the disdyakis triacontahedron

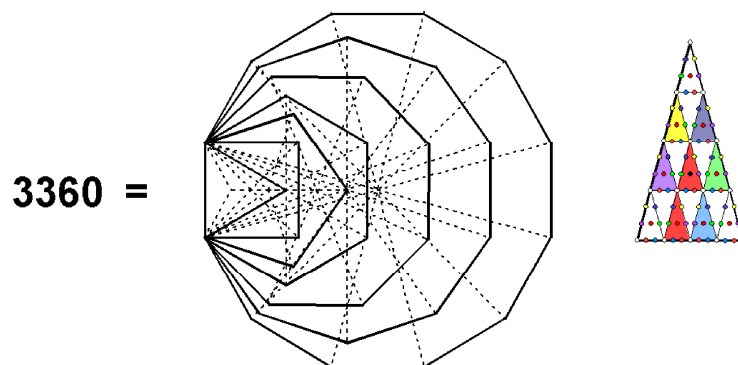


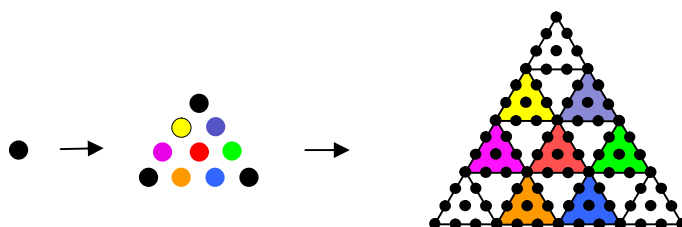
Figure 4. Constructed from 2nd-order tetractyses, the seven enfolded regular polygons constituting the inner form of the Tree of Life contain 3360 yods. This is the number of hexagonal yods in the 28 regular and semi-regular solids generated by the **62** corners of the disdyakis triacontahedron.

are:<sup>2</sup>

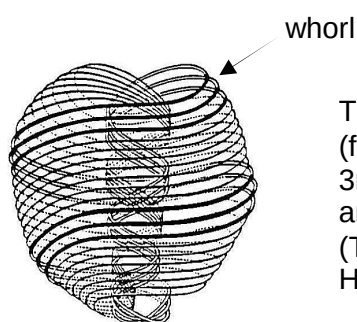
|                          |                  |            |
|--------------------------|------------------|------------|
| tetrahedron:             | $10 \times 48 =$ | 480        |
| cube:                    | $5 \times 96 =$  | 480        |
| octahedron:              | $5 \times 96 =$  | 480        |
| icosahedron:             | $1 \times 240 =$ | 240        |
| dodecahedron:            | $1 \times 240 =$ | 240        |
| rhombic dodecahedron:    | $5 \times 192 =$ | 960        |
| rhombic triacontahedron: | $1 \times 480 =$ | <u>480</u> |
| Total =                  |                  | 3360       |

This result is truly astounding for two complementary reasons:

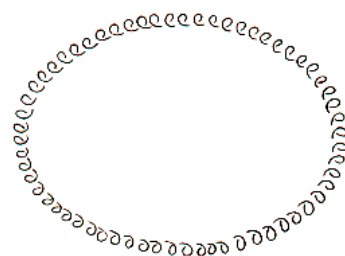
1. Divine Unity symbolised by the Pythagorean Monad, or mathematical point ("0th-order tetractys"), differentiates, firstly, into the familiar tetractys ("1st-order tetractys") with 10 yods (three corners, seven hexagonal yods), secondly, into the "2nd-order tetractys" with 85 yods (15 corners, 70 hexagonal yods), and so on:



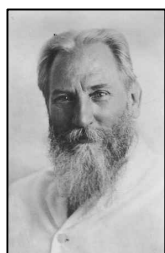
3360 is the number of yods in the seven enfolded, regular polygons constituting the inner form of the Tree of Life when their 47 sectors are each turned into the 2nd-order tetractys (Fig. 4).<sup>3</sup> We now see that the seven types of solids terminating in the disdyakis triacontahedron contain 1680 hexagonal yods (as shown on p. 14 of Article



The UPA/superstring  
(from *Occult Chemistry*,  
3rd ed., by Annie Besant  
and C.W. Leadbeater  
(Theosophical Publishing  
House, India, 1952).



The helical whorl  
has 1680 coils.



Annie Besant C.W. Leadbeater

Figure 5. The Theosophists Annie Besant and C.W. Leadbeater observed subatomic particles with the aid of a yogic siddhi called 'anima.' The basic particle of matter (identified by the author as the  $E_8 \times E_8$  heterotic superstring constituent of up and down quarks) consists of ten closed curves, or 'whorls,' that make five revolutions. Each whorl is a helical coil with 1680 turns. The number (3360) of such turns in each revolution of the ten whorls of the UPA/superstring is the number of yods in the seven enfolded polygons with 2nd-order tetractyses as their sectors.

$22^4$ ), whilst the actual numbers for the seven types of solids in the disdyakis triacontahedron total 3360 hexagonal yods, where  $3360 = 2 \times 1680$ . This is the total number of yods making up the polygonal, inner form of the Tree of Life constructed from the template of the 2nd-order tetractys. The number 3360 expresses a holistic structure *both* in the 2-dimensional space of the polygons and in the 3-dimensional space of the disdyakis triacontahedron. This marvellous, beautiful property of the polyhedron clearly demonstrating its Tree of Life basis!

2. 3360 is the number of circularly polarised standing wave oscillations made during each of the five revolutions of the ten closed curves making up the  $E_8 \times E_8$  heterotic superstring, as described by Annie Besant and C.W. Leadbeater in 1908, when they used anima to magnify subatomic particles (Fig. 5), whilst 1680 is the number of such oscillations in each curve. What this means is that, as the *completion* of the seven-fold sequence of regular and semi-regular polyhedra, the disdyakis triacontahedron *has* to be made up of the *same* number of formative degrees of freedom (hexagonal yods) as there are yods needed to represent its 2-dimensional counterpart, namely, the seven enfolded, regular polygons. Far from being a coincidence, the presence of the *same* number in two superficially different contexts reveals in an unambiguous way the **beautiful mathematical design of a transcendental, creative Intelligence**. To discover this mathematical harmony, we need to understand 'sacred geometry' — not the distorted version found in many books, which lack understanding of the fundamental principles — but the only geometry worthy of being called 'sacred,' namely, that of the Tree of Life.

Each of the 42 sides of the seven enfolded polygons has 11 yods between their ends, which number 36. The number of yods forming the boundaries of the polygons =  $11 \times 42 + 36 = 498$ . In other words, **496** yods form the sides of the polygons *between* the two endpoints of the root edge that generates them. This is the number value of the Hebrew word 'Malkuth' signifying the last Sephirah of the Tree of Life. It is yet another confirmation that the disdyakis triacontahedron is the outer (or Malkuth) aspect of the

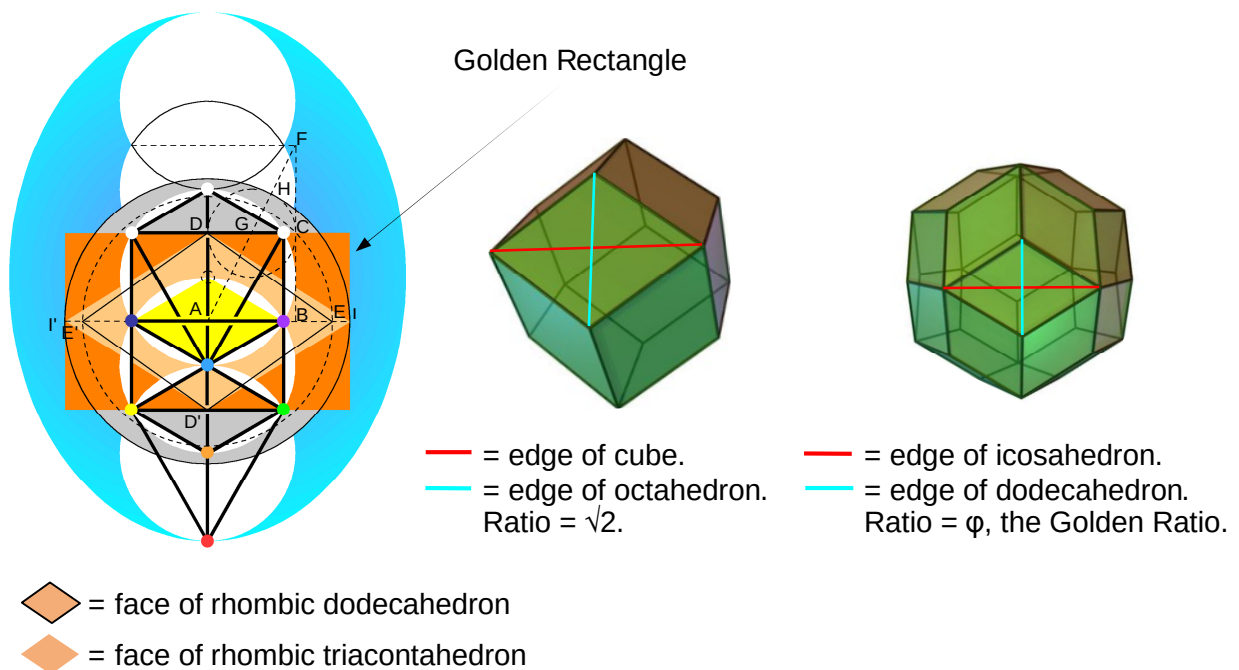


Figure 6. The faces of the rhombic dodecahedron and the rhombic triacontahedron are generated by the geometry of the Tree of Life.

inner Tree of Life. As discovered by physicists Michael Green and John Schwarz<sup>5</sup> in 1984, **496** is the dimension of the non-abelian gauge symmetry group defining superstring interactions that are free of quantum anomalies. We therefore encounter the following amazing property of the polygonal form of the inner Tree of Life blueprint: it encodes not only the oscillatory pattern of the  $E_8 \times E_8$  heterotic superstring but also the number of gauge bosons that transmit its unified force — the first as its yod population and the second as the number of yods forming its boundary between the endpoints of its generative root edge.

### 3. The rhombic dodecahedron and rhombic triacontahedron

The rhombic dodecahedron has 12 rhombic faces (Fig. 6). The longer diagonal of each face (shown as a red line in Fig. 6) is the edge of a cube and the shorter diagonal (shown as a blue line) is the edge of an octahedron. The ratio of the lengths of the longer and shorter diagonals is  $\sqrt{2} = 1.414\ldots$ . These Platonic solids are dual to each other. The two other Platonic solids that are dual to one another — the icosahedron and the dodecahedron — share an analogous property in that their edges are, respectively, the longer and shorter diagonals of the faces of the rhombic triacontahedron. Their ratio is the Golden Ratio  $\phi = 1.618\ldots$ . These rhomboids are generated in a simple way by the geometry of the Tree of Life. Fig. 6 indicates how the ten Sephiroth are the centres or points of intersection of a column of white circles. Let us take their radii as one unit. The central Pillar of Equilibrium intersects the path joining Chesed and Geburah at a point A that is one unit away from the vertical right-hand tangent BC to these circles. ABCD is a square with sides of length 1. Therefore, its diagonal  $AC = \sqrt{(1^2 + 1^2)} = \sqrt{2}$ . With A as centre, draw a circle passing through C of radius  $\sqrt{2}$  (shown as a dashed line in Fig. 6). It intersects the line drawn along AB at E. E' is the corresponding point on the other side of the central pillar.  $EE' = 2\sqrt{2}$ . The central pillar intersects the path joining Netzach and Geburah at D'.  $DD' = 2$ . Therefore,  $EE'/DD' = 2\sqrt{2}/2 = \sqrt{2}$ . We find that the rhombus DED'E' has the same shape as the rhombic face of the rhombic dodecahedron.

Extend the tangent at B to the point F, where  $BC = CF = 1$ . Then,  $BF = 2$  and  $AF = \sqrt{(2^2 + 1^2)} = \sqrt{5}$ . The line AF intersects CD at G, where  $AG = GF = \sqrt{5}/2$ . With G as centre, draw a circle of radius  $\frac{1}{2}$ . It intersects AF at H, where  $AH = \sqrt{5}/2 + \frac{1}{2} = (\sqrt{5}+1)/2 = \phi$ , the Golden Ratio. With A as centre, draw a circle of radius AH. It intersects the extension of AB at I, where  $AI = \phi$ . I' is its counterpart on the other side of the central pillar.  $II' = 2\phi$ . Therefore,  $II'/DD' = 2\phi/2 = \phi$ . The rhombus DI D'I' has the same shape as the rhombic face of the rhombic triacontahedron. What manifests finally as the fruit of the Tree of Life, namely, the disdyakis triacontahedron with golden rhombic faces, was within it as their seed shape from the very beginning!

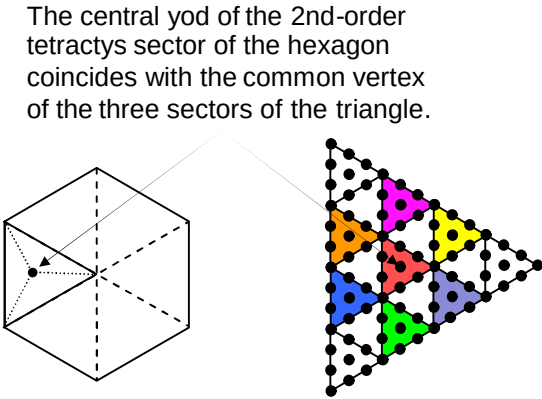
### References

- <sup>1</sup> Phillips, Stephen M. *The Mathematical Connection between Religion and Science* (to be published).
- <sup>2</sup> The hexagonal yod populations of these solids are taken from p. 6 of Article 22: "The Disdyakis Triacontahedron as the 3-dimensional Counterpart of the Inner Tree of Life" at: <http://www.smpillips.8m.com/article22.pdf>.
- <sup>3</sup> Proof: The 2nd-order tetractys has 85 yods, of which 13 yods line each of its sides. When each of the  $n$  triangular sectors of an  $n$ -sided, regular polygon are turned into a 2nd-order tetractys, there are  $(85 - 13n = 72n + 1)$  independent yods per sector of the polygon. Its yod population =  $72n + 1$ , where "1" denotes the yod at the centre of the polygon. The polygonal form of the inner Tree of Life consists of a triangle, square, pentagon, hexagon, octagon, decagon and dodecagon. They are enfolded in one another and share the same base, or what the author has called the "root edge," as they should be thought of as growing out of this fundamental line joining Daath and Tiphareth in the Tree of Life. When the seven

separate polygons are superposed on one another in their enfolded state, corresponding members of the set of 13 yods forming what becomes their shared side coincide and therefore must not be counted separately in a calculation of their yod population. Below are listed the yod populations of each polygon and (except for the triangle) their numbers of yods outside the root edge:

| Polygon   | n  | Number of yods = $72n + 1$ | Number of yods outside root edge |
|-----------|----|----------------------------|----------------------------------|
| triangle  | 3  | 217                        |                                  |
| square    | 4  | 289                        | $289 - 13 = 276$                 |
| pentagon  | 5  | 361                        | $361 - 13 = 348$                 |
| hexagon   | 6  | 433                        | $433 - 13 = 420$                 |
| octagon   | 8  | 577                        | $577 - 13 = 564$                 |
| decagon   | 10 | 721                        | $721 - 13 = 708$                 |
| dodecagon | 12 | 865                        | $865 - 13 = 852$                 |
|           |    |                            | Total = 3385                     |

Inspection of Fig. 4 reveals that the tip of the triangle viewed with the root edge as its base is also the centre of the hexagon (the triangle is simply a triangular sector of the hexagon). Similarly, the tip of the



The central yod of the 2nd-order tetractys sector of the hexagon coincides with the common vertex of the three sectors of the triangle.

pentagon is the centre of the decagon. With 2nd-order tetractyses as their sectors, the centroid of the triangle where corners of its three 2nd-order tetractyses meet is also the central yod of the tetractys at the centre of the 2nd-order tetractys constituting a sector of the hexagon (see diagram above). The 11 yods between corners on each of the two sides of the triangle outside its shared base coincide with yods on the sides of this sector of the hexagon. There are  $(1 + 1 + 1 + 2 \times 11 = 25)$  yods in the total population calculated above that coincide with yods belonging to other polygons (these are the only yods occupying the same positions). In determining the yod population when the separate polygons are superposed, these yods must be subtracted in order to avoid double-counting

Therefore, the yod population of the seven enfolded polygons constructed from 2nd-order tetractyses =  $3385 - 25 = 3360$ .

<sup>4</sup> Ref. 2, p. 14.

<sup>5</sup> Green, M.B. & Schwarz, J.H. "Anomaly cancellations in supersymmetric  $d = 10$  gauge theory and superstring theory." Physics Letters, B149, 117.