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Stephen M. Phillips

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ARTICLE 49

How Some Sacred Geometries are Equivalent Maps of All Levels of Reality

"As above, so below."

by

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ABSTRACT

The triangular array of ten points, or tetractys, at the heart of Pythagoras' philosophy can be regarded as but the first member of an infinite sequence of higher order tetractyses. The mathematical realisation of the Hermetic axiom "as above, so below" is the Cosmic Tetractys in which the centre of a 2nd-order tetractys is another 2nd-order tetractys. Its 91 1st-order tetractyses represent the 91 subplanes of the seven cosmic planes of consciousness expounded by Theosophy. As the ten points of the tetractys denote the ten Sephiroth of the Tree of Life, the Cosmic Tetractys is equivalent to 91 overlapping Trees of Life (CTOL) with 550 Sephirothic emanations. As well as its outer form known to Kabbalists, the Tree of Life has an inner form consisting of two enfolded, similar sets of seven regular polygons that share one 'root edge.' Constructed from tetractyses, a unique set of twelve of these separate polygons, together with this root edge, have 91 corners and 550 yods. The Inner Tree of Life encodes the replication of its outer form to encompass all levels of reality. One set of seven polygons represents the cosmic physical plane and the five others represent the six cosmic superphysical planes. As independent evidence supporting this interpretation, the gematria number value of the Hebrew name of the Mundane Chakra of Malkuth (the physical level of the Tree of Life) determines the geometrical composition of the 49 Trees of Life that map the cosmic physical plane, whilst this map embodies the number value of Malkuth when constructed from tetractyses. The Sri Yantra is shown to be the counterpart of CTOL because the numbers 91 and 550 are embodied in its geometry. They are also embodied in the five Platonic solids because 550 points, lines & triangles are needed to construct their 50 faces, whilst the 90 interior triangles formed by their vertices and shared centre have 270 sectors with 91 corners. Constructed from tetractyses, the faces of the dodecahedron contain 550 points other than corners of tetractyses. The faces of the first four Platonic solids, which the ancient Greeks believed were the shapes of the elements Earth, Water, Air & Fire, are constructed from the 248 corners & sides of 120 triangles, showing how they embody the dimension 248 of the superstring gauge symmetry group E_8 . Previous work established that the outer form of the polyhedral version of the Tree of Life is the disdyakis triacontahedron. Its 60 vertices surrounding an axis passing through two opposite vertices of a certain type are corners of 15 polygons. Including these two vertices, they possess 550 vertices, sides & triangles when their sectors are divided into three triangles. The eight polygons in one half of the polyhedron are composed of 299 geometrical elements. This is the number of Sephirothic emanations in the 49 Trees of Life mapping the cosmic physical plane. The 251 elements in the remainder of the polyhedron correspond to the 251 emanations in the 42 Trees of Life that map the six cosmic superphysical planes. The interior geometry of the disdyakis triacontahedron therefore represents CTOL. This is confirmed by the fact that the number of yods in the 15 polygons surrounding the centre of the polyhedron is the number of yods on the central pillar of CTOL between its apex and nadir when its triangles are tetractyses.

Table 1. Gematria number values of the ten Sephiroth in the four Worlds.

	SEPHIRAH	GODNAME	ARCHANGEL	ORDER OF ANGELS	MUNDANE CHAKRA
1	Kether (Crown) 620	EHYEH (I am) 21	Metatron (Angel of the Presence) 314	Chaioth ha Qadesh (Holy Living Creatures) 833	Rashith ha Gilgalim First Swirlings. (Primum Mobile) 636
2	Chokmah (Wisdom) 73	YAHVEH, YAH (The Lord) 26, 15	Raziel (Herald of the Deity) 248	Auphanim (Wheels) 187	Masloth (The Sphere of the Zodiac) 140
3	Binah (Understanding) 67	ELOHIM (God in multiplicity) 50	Tzaphkiel (Contemplation of God) 311	Aralim (Thrones) 282	Shabathai Rest. (Saturn) 317
	Daath (Knowledge) 474				
4	Chesed (Mercy) 72	EL (God) 31	Tzadkiel (Benevolence of God) 62	Chasmalim (Shining Ones) 428	Tzadekh Righteousness. (Jupiter) 194
5	Geburah (Severity) 216	ELOHA (The Almighty) 36	Samael (Severity of God) 131	Seraphim (Fiery Serpents) 630	Madim Vehement Strength. (Mars) 95
6	Tiphareth (Beauty) 1081	YAHVEH ELOHIM (God the Creator) 76	Michael (Like unto God) 101	Malachim (Kings) 140	Shemesh The Solar Light. (Sun) 640
7	Netzach (Victory) 148	YAHVEH SABAOOTH (Lord of Hosts) 129	Haniel (Grace of God) 97	Tarshishim or Elohim 1260	Nogah Glittering Splendour. (Venus) 64
8	Hod (Glory) 15	ELOHIM SABAOOTH (God of Hosts) 153	Raphael (Divine Physician) 311	Beni Elohim (Sons of God) 112	Kokab The Stellar Light. (Mercury) 48
9	Yesod (Foundation) 80	SHADDAI EL CHAI (Almighty Living God) 49, 363	Gabriel (Strong Man of God) 246	Cherubim (The Strong) 272	Levanah The Lunar Flame. (Moon) 87
10	Malkuth (Kingdom) 496	ADONAI MELEKH (The Lord and King) 65, 155	Sandalphon (Manifest Messiah) 280	Ashim (Souls of Fire) 351	Cholem Yesodeth The Breaker of the Foundations. The Elements. (Earth) 168

The Sephiroth exist in the four Worlds of Atziluth, Beriah, Yetzirah and Assiyah. Corresponding to them are the Godnames, Archangels, Order of Angels and Mundane Chakras (their physical manifestation, traditionally symbolised by celestial bodies). This table gives their number values obtained by the ancient practice of gematria, wherein a number is assigned to each letter of the alphabet, thereby giving to a word a number value that is the sum of the numbers of its letters.

*(All numbers in this table referred to in the article are written in **boldface**).*

1. The Cosmic Tetractys

At the heart of the ancient Pythagorean teachings was the triangular array of ten points known as the tetractys (Fig. 1).

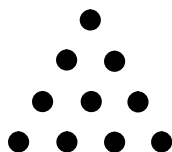


Figure 1. The tetractys.

The modern academic view is that it represented what the Pythagoreans regarded as the perfect number 10 (Decad) as the fourth, so-called 'polygonal number,' the four rows of one, two, three & four dots symbolising, respectively, a mathematical point, the two points at the ends of a straight line, the corners of a triangle and the four vertices of a tetrahedron. However, it was far more than that, as the oath made by members of Pythagoras' mystery school testifies:

"I swear by the discoverer of the tetractys,
Which is the spring of all our wisdom,
The perennial fount and root of Nature."

The seminal importance of the tetractys to Pythagoreans was due to this figure being not merely symbolic, as most mathematicians have wrongly believed, but the actual template of sacred geometry that transforms the latter into numbers of fundamental significance to the mathematical design of the universe and therefore having scientific meaning. The notion of design, with its implication of a Designer, is anathema, of course, to many scientists who hold to the materialistic paradigm that the universe sprung

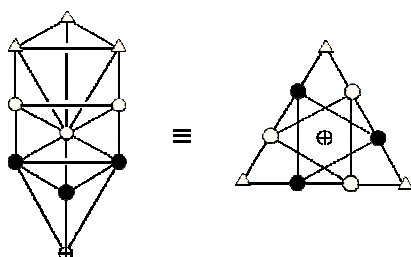


Figure 2. The one-to-one correspondence between the ten Sephiroth of the Tree of Life and the ten points (yods) of the tetractys.

into existence without the assistance of God. Hence, they would reject the claim of the Pythagoreans that the tetractys has a profound, metaphysical meaning that reveals the mysteries of the universe. The author's previous 48 research articles have demonstrated beyond doubt that this view is wrong. The tetractys is a representation of the Kabbalistic Tree of Life, each of its ten points (or 'yods,' from the

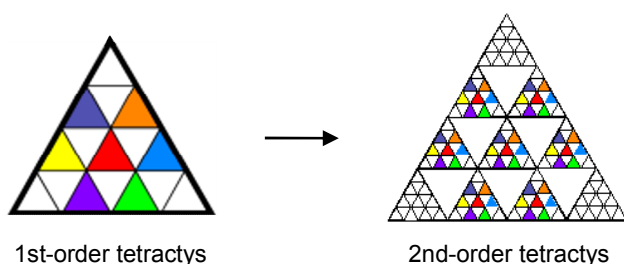


Figure 3. The seven coloured triangles in the 1st-order tetractys differentiate into the **49** coloured triangles of the 2nd-order tetractys.

Hebrew name 'yod' of the *tenth* letter of the Hebrew alphabet) corresponding to one of the ten Sephiroth (Fig. 2). The yods either at the corners of a hexagon or at its centre will be called 'hexagonal yods.' They symbolize the seven Sephiroth of Construction. The yods at the corners of the tetractys denote the Supernal Triad of Kether, Chokmah and Binah and the central hexagonal yod denotes Malkuth.

Suppose that we replace each point of a tetractys by a triangle. The motive behind this is to express the idea that each point of the tetractys ('1st-order tetractys') is a *potential tetractys in itself* and a member of a higher-order tetractys, or '2nd-order tetractys' (Fig. 3). Each triangle is then turned into a copy of the whole of which it was a constituent. All the triangles in the 1st-order triangles at the corners of the 2nd-order tetractys shown in Fig. 3 have been left white in order to conform to the white triangles in the original 1st-order tetractys. The seven coloured triangles in the 1st-order tetractys become ($7^2=49$) coloured triangles in the 2nd-order tetractys. There are 17 points along each side of the 2nd-order tetractys that are corners of 16 triangles. The number of corners of the triangles on its boundary is **48**.

This is the number value of *Kokab*, the Mundane Chakra of Hod. The number **48** is always a basic measure of the global nature of a holistic system, as has been demonstrated in many previous articles and as will be illustrated in subsequent sections. A triangular array of **153** points (Fig. 4), 17 points along each side, comprises 300 sides of 100 triangles that form a 2nd-order tetractys. Each of its ten 1st-order tetractyses is made up of the **15** corners & 30 sides of ten triangles, that is, 55 geometrical elements, where

$$55 = \begin{array}{c} 1 \\ 2 \ 3 \\ 4 \ 5 \ 6 \\ 7 \ 8 \ 9 \ 10. \end{array}$$

This demonstrates how the Decad determines the geometrical composition of a 1st-order tetractys whose yods are triangles. As $150 = 15 \times 10$, YAH, the Godname of Chokmah with number value **15** and ELOHIM SABAOTH, the Godname of Hod with number value **153**, prescribe the geometrical array of points

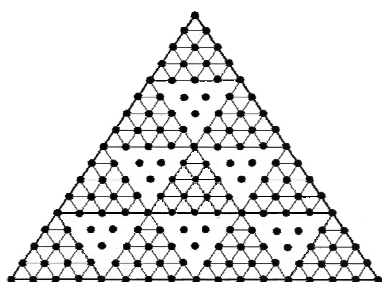


Figure 4. ELOHIM SABAOTH, the Godname of Hod with number value **153**, prescribes the triangular array of **153** points underlying the 10 1st-order tetractyses of the 2nd-order tetractys.

underlying the 2nd-order tetractys, the ten 1st-order tetractyses each having **15** corners. The ten *separate* 1st-order tetractyses have ($10 \times 55 = 550$) geometrical elements that become 535 geometrical elements in the 2nd-order tetractys when their corners coincide, **15** corners disappearing in the process. Including the 18 points in the six triangular gaps between 1st-order tetractyses, the triangular array consists of ($18 + 535 = 553$) geometrical elements. Starting with three points as the three corners of a triangle, **550** more elements (150 corners, 300 sides & 100 triangles) are needed to create the triangular array, where

$$550 = \begin{array}{c} 55 \\ 55 \ 55 \\ 55 \ 55 \ 55 \\ 55 \ 55 \ 55 \ 55 \end{array} = \begin{array}{c} 10 \\ 20 \ 30 \\ 40 \ 50 \ 60 \\ 70 \ 80 \ 90 \ 100. \end{array}$$

This demonstrates how the Decad determines the geometrical composition of a 2nd-order tetractys as well as a 1st-order tetractys. The number 550 will manifest in various sacred geometries discussed later.

Let us next take this transformation a step further but with the difference that only the central 1st-order tetractys in the 2nd-order tetractys is replaced by the 2nd-order tetractys (Fig. 5). This generates what will be called the 'Cosmic Tetractys.' Its central 2nd-order tetractys, which denotes the Sephirah Malkuth, contains ($7 \times 7 = 49$) coloured triangles symbolizing the seven Sephiroth of Construction. **49** is the number

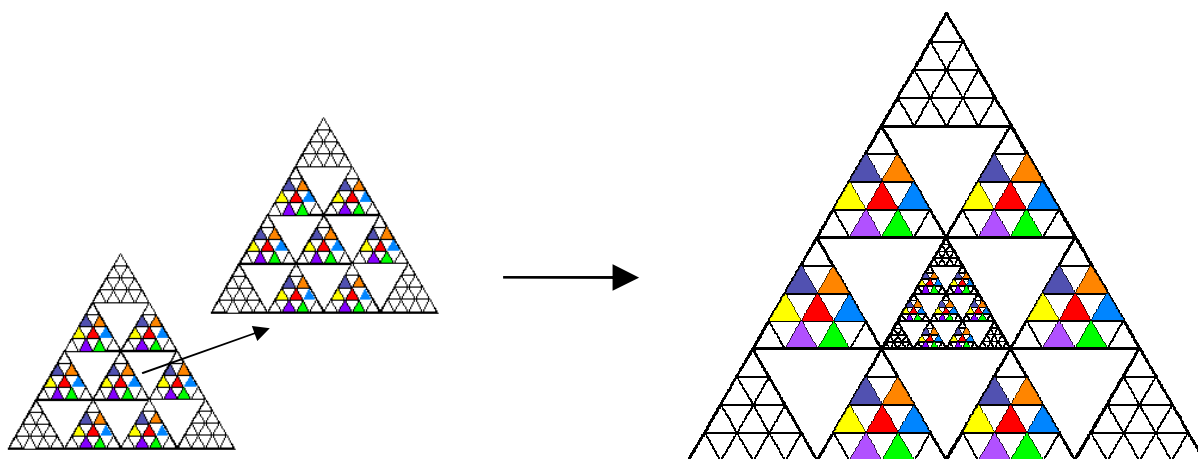


Figure 5. Replacing the central 1st-order tetractys of a 2nd-order tetractys by a 2nd-order tetractys generates the Cosmic Tetractys.

value of EL ChAI, the Godname of Yesod. The six 1st-order tetractyses surrounding it refer to the six Sephiroth of Construction above Malkuth and contain ($6 \times 7 = 42$) coloured triangles. The seven Sephiroth of Construction are expressed in the Cosmic Tetractys by ($49 + 42 = 91$) coloured triangles, where

$$91 = 1^2 + 2^2 + 3^2 + 4^2 + 5^2 + 6^2.$$

Because the square of any integer n is the sum of the first n odd integers, 91 is the sum of ($1+2+3+4+5+6=21$) odd integers. This is the number value of EHYEH, the Godname of Kether. Explicitly,

$$91 = \begin{array}{l} 1 \\ 1 + 3 \\ 1 + 3 + 5 \\ 1 + 3 + 5 + 7 \\ 1 + 3 + 5 + 7 + 9 \\ 1 + 3 + 5 + 7 + 9 + 11 \end{array} = 65 + 26$$

15 integers form the boundary of the triangular array, showing how YAH prescribes this number. YAH also prescribes it because a **15**-sided polygon with its sectors turned into 1st-order tetractyses has 91 yods. The sum of the integers is **65**, the remaining six integers inside the boundary adding to **26**. **65** is the

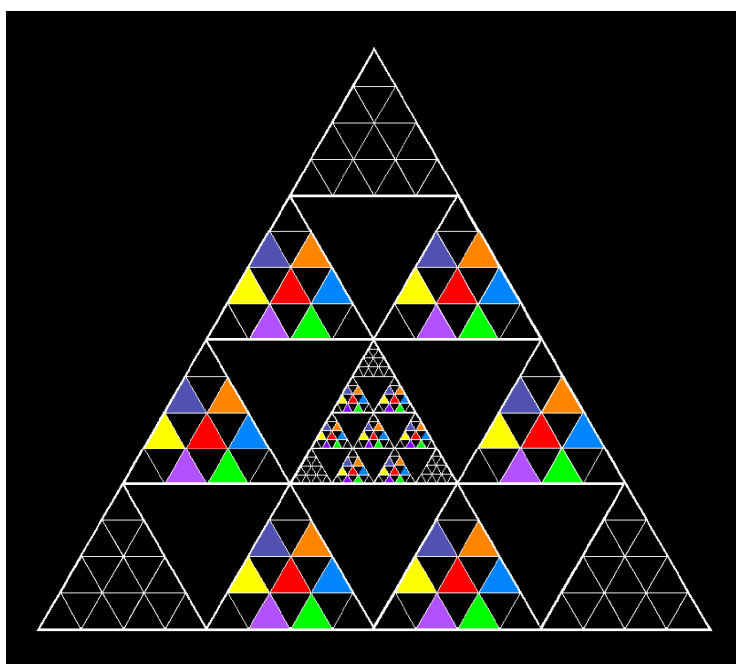


Figure 6. The Cosmic Tetractys. The 91 coloured triangles represent 7-fold differentiations of the 7 Sephiroth of Construction denoted by the central 2nd-order tetractys and by the six 1st-order tetractyses that surround it. They are expressed by the compound Divine Name ADONAI TETRAGRAMMATON.

number value of ADONAI (“My Lord”) and **26** is the number value of YAHWEH. Out of reverence for the holy nature of YHVH (Tetragrammaton) and because most Jewish denominations teach that it is forbidden to utter the Name of God except by the High Priest in the Temple, Jews substitute it in prayers with ADONAI. 91 is the number value of ADONAI TETRAGRAMMATON.

The fact that the centre of the Cosmic Tetractys is another 2nd-order tetractys like itself can be regarded as the geometrical realisation of the Hermetic principle “As above, so below.” As a map of all levels of consciousness (as we shall shortly see) — the Cosmic Tetractys is somewhat analogous to a hologram. This reproduces a three-dimensional image of a scene, each point in the hologram containing light from the whole of the original scene. In principle, the latter can be reproduced from any part of the hologram, however small, although in practice, the image becomes fuzzier because diffraction causes a loss of resolution. *All information about the whole holographic image is contained in any part.* The purist may object that this analogy between a hologram and the Cosmic Tetractys breaks down because only the central 2nd-order tetractys is identical to the parent one — its nine other 1st-order tetractyses remain such in the Cosmic Tetractys. The criticism is misplaced. Every triangle representing a Sephirah is potentially a 1st-order tetractys and therefore also a 2nd-order tetractys. It is this fundamental property that is analogous to a hologram, not the geometry of the Cosmic Tetractys *per se*.

2. The Cosmic Tree of Life

The 91 coloured triangles in the Cosmic Tetractys symbolize all possible differentiations of the seven

Sephiroth of Construction subject to the requirement of consistency with the Hermetic principle of correspondences that all their **49** differentiations should appear as well in the last one, Malkuth. As a triangle is a potential 1st-order tetractys, which is simply a Pythagorean representation of the Tree of Life, it is deduced that the seven Sephiroth of Construction require 91 Trees of Life represent their cosmic manifestation. The Tree of Life counterpart of the Cosmic Tetractys therefore consists of 91 Trees of Life that overlap one another (Fig. 7). This scheme will be called the 'Cosmic Tree of Life,' or CTOL. As the yod at the centre of a tetractys corresponds to Malkuth in the Tree of Life, the cosmic physical level of CTOL corresponding to Malkuth consists of the lowest **49** overlapping Trees of Life, each one denoted by one of the 49 coloured triangles (potential tetractyses) that form the central yod (Malkuth) of the Cosmic Tetractys. The cosmic superphysical region of CTOL is defined by the set of 42 Trees of Life above the lowest **49** Trees of Life. They correspond to the 42 larger, coloured triangles (potential tetractyses) in Fig. 6 symbolizing the six Sephiroth of Construction above Malkuth.

A THEOSOPHICAL INTERPRETATION

H.P. Blavatsky, one of the founders of the Theosophical Society, stated in her book *The Secret Doctrine* that Creation is divided into seven great planes of consciousness. Many of her ideas, which her book proved are found in the creation mythologies of ancient religions like Judaism and Hinduism, were developed by later Theosophical writers, such as Annie Besant and Charles W. Leadbeater. In particular, Alice Bailey gave a more precise and detailed formulation of the Theosophical classification of the planes. We shall follow her terminology, which is now commonly used in mainstream, Theosophical literature.

The seven cosmic planes of consciousness are:

- 1) Adi, or Divine, plane;
- 2) Anupadaka, or Monadic, plane;
- 3) Atmic plane;
- 4) Buddhic plane;
- 5) Mental plane;
- 6) Astral plane;
- 7) Physical plane.

Each cosmic plane is divided into seven cosmic subplanes. The seven subplanes of the cosmic physical plane are called 'solar planes.' The word solar was used not to imply any connection with the Sun but to convey a loose analogy (that is, not to be regarded in any literal sense) between the difference between the Solar System and the rest of the universe and the distinction between the cosmic physical plane and the six cosmic superphysical planes of consciousness. The solar planes, too, have the names listed above, e.g., Theosophists speak of the 'solar physical plane,' the solar astral plane,' etc. Each solar plane is further divided into seven solar subplanes. The solar physical plane consists of seven solar physical subplanes; the solar astral plane consists of seven solar astral subplanes, etc. The seven solar planes of the cosmic physical plane have ($7 \times 7 = 49$) solar subplanes and the six cosmic superphysical planes (astral→adi) have ($6 \times 7 = 42$) subplanes. All seven cosmic planes have ($49 + 42 = 91$) subplanes.

The seven planes (cosmic or solar) denote primary modalities of consciousness that correspond in a one-to-one way to the seven Sephiroth of Construction:

Adi	→	Chesed,
Anupadaka	→	Geburah,
Atmic	→	Tiphareth,
Buddhic	→	Netzach,
Mental	→	Hod,
Astral	→	Yesod,
Physical	→	Malkuth.

Only the four lowest Sephiroth of the Tree of Life: Malkuth, Yesod, Hod and Netzach, are at present components of normal consciousness. They correspond in the human personality to the four psychological functions of, respectively, sensing, feeling, thinking and intuiting, identified by the great psychoanalyst, C. J. Jung. Atmic, or mystical, consciousness corresponds formally to what Jung called the 'transcendent function of the psyche.' It is the expression of Tiphareth. A one-to-one association similarly exists between the seven subplanes of a cosmic or solar plane and the seven Sephiroth of Construction. It must be emphasized that Theosophical planes are *not* synonymous with the latter. The Kabbalistic notion of the Sephiroth is more fundamental than the Theosophical concept of planes. The latter are modalities of consciousness that express the particular quality of their corresponding Sephirah.

Comparison of the Theosophical scheme of planes of consciousness with the Cosmic Tetractys shown in Fig. 6 establishes the following set of correspondences (▲ = coloured triangle):

obviously not the 91-tree but 91 overlapping TOLs.

(3) A 'tree level' is any one of the seven horizontal divisions of a TOL in CTOL marked by SLs that are shared by adjoining TOLs (Fig. 8). Tree levels are thus defined by the five SLs on the central Pillar of Equilibrium of the TOL, the Path linking its Chokmah and Binah and the Path joining its Netzach and Hod, which are Chokmah and Binah of the next lower TOL. Each TOL has seven tree levels shared by adjacent, overlapping TOLs. The horizontal Path linking Chesed and Geburah of a TOL does not define a tree level because these Sephiroth are not shared by adjacent TOLs. Daath defines a tree level provided that it is Yesod of the next higher TOL. No tree level is therefore defined for Daath of the 91st TOL because that is the last one in CTOL. The scientific meaning of the 25 tree levels of the 7-tree representing the physical plane (the physical universe) is that they denote the 25 spatial dimensions of the **26**-dimensional space-time continuum predicted by quantum mechanics for so-called 'spinless bosonic strings.' Tree levels may be thought of as the rungs of the 'Jacob's ladder' referred to in the bible when it is interpreted as a set of overlapping TOLs that

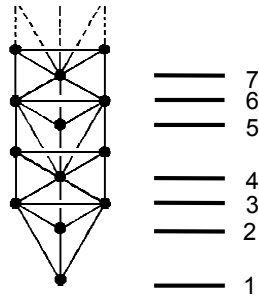


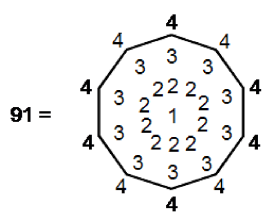
Figure 8. Tree levels on overlapping Trees of Life.

map all levels of reality.

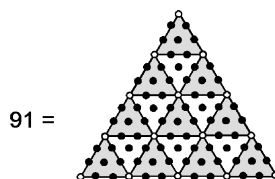
The structure of CTOL is described by the following formulae:

1. Kether of the nth TOL is number
 $S(n) = 6n + 5$ ($1 \leq n \leq 90$; $S(91) = 550$)
2. Kether of the nth TOL is the $(2n+3)$ th SL on the central Pillar of Equilibrium ($1 \leq n \leq 90$); Kether of the 91st TOL is the 184th SL on the central pillar.
3. The nth SL on the central pillar is number
 $C(n) = 3n - 4$ ($3 \leq n \leq 183$; $C(1) = 1$, $C(2) = 2$, $C(184) = 550$)
5. Kether of the nth TOL is tree level number
 $L(n) = 3n + 4$ ($1 \leq n \leq 90$; $L(91) = 276$)
6. Number of tree levels up to the nth SL on the central Pillar is
 $T(n) = (3n-2)/2$ (n even)
 $= (3n-1)/2$ (n odd)
7. The n-tree has $(n+1)$ Upper and Lower Faces.
8. Number of Paths in the n-tree is
 $P(n) = 16n + 6$ (n overlapping TOLs)
 $= 16n + 9$ (n-tree)

The 91 overlapping TOLs in CTOL has 550 SLs. Compare this with the facts established earlier that the ten 1st-order tetractyses that form the 2nd-order tetractys have 550 geometrical elements when they are separate and that 550 geometrical elements are needed to construct its underlying triangular array of **153** points, starting from the three corners of a triangle. According to formula 1, the **49**-tree mapping the cosmic physical plane has $S(49) = 299$ SLs. Hence, there are 251 SLs above it. The 7-tree has 47 SLs, so that its apex is the 504th SL from the top of CTOL. The lowest TOL is the 1-tree with 11 SLs, so that its top is the 540th from the top of CTOL. The Decad determines the number 91 because a decagonal array of the integers 1, 2, 3 & 4 symbolised by the tetractys add up to 91:



As the 13th triangular number, 91 is the number of points in the triangular array underlying a 1st-order tetractys in which each triangle is a tetractys:



The odd integers in the sum of the first 13 integers:

$$91 = 1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + 9 + 10 + 11 + 12 + 13$$

add up to **49** and the even integers sum to 42. This arithmetic division created by the even and odd integers mirrors the division of the seven cosmic planes into the **49** subplanes of the cosmic physical plane and the 42 subplanes of the six cosmic superphysical planes.

The Godname ELOHA with number value **36** prescribes CTOL because 91 is the sum of the **36** integers (**15** even, **21** odd) in the array:

```

      6
    5 5 5
  4 4 4 4 4
3 3 3 3 3 3 3
2 2 2 2 2 2 2 2
1 1 1 1 1 1 1 1 1 1

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ELOHIM, the Godname of Binah with number value **50**, prescribes the 550 SLs in CTOL because $550 = 10 \times 55$, where

$$55 = 1^2 + 2^2 + 3^2 + 4^2 + 5^2,$$

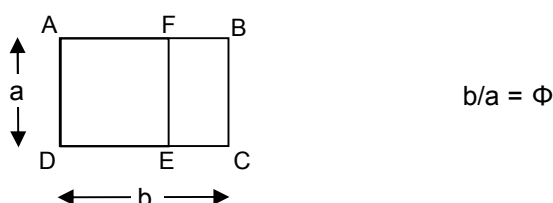
i.e., 550 is the sum of $(10 \times 5 = 50)$ squares of the integers 1-5. Therefore,

$$\begin{aligned}
 550 &= 10 \\
 &10 + 30 \\
 &10 + 30 + 50 \\
 &10 + 30 + 50 + 70 \\
 &10 + 30 + 50 + 70 + 90.
 \end{aligned}$$

The Godname YAH with number value **15** prescribes the number 550 as the sum of **15** numbers. We saw earlier how the Decad determines the number 550 as 10×55 , where 55 is the sum of the first ten integers. 55 is also the tenth, so-called 'Fibonacci number.' Named after the 13th century Italian mathematician Leonardo of Pisa, also called Fibonacci, these are numbers appearing in the infinite sequence of integers:

1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144 ...

They have the property that each is the sum of the two previous numbers. They are known to be present in the phyllotaxis of many flowers and plants. The ratio of successive Fibonacci numbers converges towards the Golden Ratio $\Phi = (1 + \sqrt{5})/2 \approx 1.6180339887...$ This is the ratio of adjacent sides of the Golden Rectangle ABCD:



It has the remarkable property that, when a square ADEF is cut away from it with a side equal to the shorter side of the Golden Rectangle, the sides of the remaining rectangle BCEF has the same proportion as those of the original rectangle and therefore it is another Golden Rectangle.

3. Encoding of CTOL in the Inner Tree of Life

Polygonal representation of the n-tree

When the n sectors of an n -sided polygon (not necessarily regular) are each turned into tetractyses, six yods are added per sector, so that $(6n+1)$ yods are generated, the number "1" referring to its centre. According to formula 1 given above, the number of SLs in the n -tree is

$$S(n) = 6n + 5.$$

There are four SLs beyond Chesed of the n th TOL up to its top. Therefore, the number of SLs up to Chesed of the n th TOL $= S(n) - 4 = 6n + 1$, where the number '1' denotes the lowest SL and six SLs are added for each overlapping TOL: $S(n+1) - S(n) = 6$. But $(6n+1)$ is the number of yods in an n -sided polygon. Such a tetractys-constructed polygon is therefore a representation of n overlapping TOLs as far as its highest Chesed. The central yod corresponds to the lowest SL, the pair of hexagonal yods on each side of the polygon, being unshared by adjacent sectors, correspond to Chesed and Geburah of each TOL because these are unshared with adjacent TOLs. The yods at the corners of the polygon correspond to Yesod of each TOL and the hexagonal yods at the centres of the sectors correspond to each Malkuth, except for the lowest one, which is denoted by the centre of the polygon. Enclosing the n -sided polygon in

from the bottom of the table. They are separated by the root edge, one set of seven polygons being arranged in the reverse sequence of the other set (the issue of other possible arrangements will be addressed later). Reading upwards from the base of the table, we find:

1. the first five polygons have **26** vertices or tetractyses and 161 yods. Compare this with the 161 SLs of the **26**-tree;
2. the first seven polygons have 295 yods. Chesed of the **49th** TOL is the 295th SL;
3. the first seven polygons & the root edge have 299 yods. Kether of the **49th** TOL is the 299th SL;
4. *the first 12 polygons & the root edge have 550 yods and 91 vertices* (from a formal, mathematical point of view, the endpoints of the root edge count as vertices). CTOL has 550 SLs and 91 TOLs.

Any set of five polygons with N corners will have a yod population obeying the formula $S(N) = 6N + 5$ for the number of SLs in the N-tree because

$$\sum_{\text{set}} (6n+1) = 6 \sum_{\text{set}} n + 5 = 6N + 5,$$

where

$$N \equiv \sum_{\text{set}} n$$

is the number of corners of the five polygons. Therefore, it is not surprising that the yod population of the first five polygons obeys this formula. However, what is interesting is that this set of polygons has **26**

POLYGON	NUMBER OF YODS	RUNNING TOTAL	NUMBER OF TREES
Dodecagon	73	594	
Decagon	61	521	→ 86
Octagon	49	460	→ 76 ✓
Hexagon	37	411	
Pentagon	31	374	
Square	25	343	
Triangle	19	318	
Root edge	4	299	→ 49
Triangle	19	295	
Square	25	276	
Pentagon	31	251	→ 41
Hexagon	37	220	→ 36 ✓
Octagon	49	183	
Decagon	61	134	
Dodecagon	73	73	
POLYGON	NUMBER OF YODS	RUNNING TOTAL	NUMBER OF TREES
Triangle	19	594	
Square	25	575	→ 95
Pentagon	31	550	→ 91 ✓
Hexagon	37	519	
Octagon	49	482	
Decagon	61	433	
Dodecagon	73	372	
Root edge	4	299	→ 49
Triangle	19	295	
Square	25	276	
Pentagon	31	251	→ 41
Hexagon	37	220	→ 36 ✓
Octagon	49	183	
Decagon	61	134	
Dodecagon	73	73	
POLYGON	NUMBER OF YODS	RUNNING TOTAL	NUMBER OF TREES
Dodecagon	73	594	
Decagon	61	521	→ 86
Octagon	49	460	→ 76 ✓
Hexagon	37	411	
Pentagon	31	374	
Square	25	343	
Triangle	19	318	
Root edge	4	299	→ 49
Dodecagon	73	295	
Decagon	61	222	
Octagon	49	161	→ 26
Hexagon	37	112	
Pentagon	31	75	
Square	25	44	
Triangle	19	19	

vertices, where **26** is the number value of YAHWEH, and 161 yods, which is the number of SLs in the **26**-tree. What is even more interesting (in fact, remarkable) is that the seven polygons and the root edge have the same number of yods as there are SLs in the **49**-tree, which maps the **49** subplanes of the seven planes of the cosmic physical plane! The four yods of the root edge therefore denote Kether, Chokmah, Binah and Daath of the **49th** TOL. What is most interesting of all is that there exists a subset of the 14 polygons that — together with the root edge — have not only 91 vertices symbolizing the 91 TOLs of CTOL but also 550 yods that denote their 550 SLs. That subset is the set of the first 12 polygons and the root edge. This is amazing, for even if it were coincidence that a set of polygons can be found that contains 550 yods when the root edge is included, it is highly implausible that they would by chance possess 91 vertices as well! Nor is it plausible that it could be just coincidence that the number of SLs in the **49**-tree is equal to the number of yods in the root edge and all seven polygons of the Inner TOL.

Twelve of the 14 polygons collectively encode the self-replication of a single TOL into CTOL as a map of all levels of reality. These 12 enfolded polygons have **67** corners (**65** outside the root edge) and **76** corners and centres of 88 tetractyses. This is how the respective numbers of Binah, ADONAI and YAHWEH ELOHIM prescribe the polygonal encoding of CTOL (the complete prescription by all Godnames is given in Article 4¹). Moreover, only this particular combination of polygons has such a property, because only the triangle and square have the necessary seven vertices that must be excluded from

Figure 11. Alternative, possible orderings of polygons belonging to the Inner Tree of Life. Allowed numbers of overlapping TOLs in the last column are shown ticked. The thick lines separate one set of seven polygons & the root edge from the other set. The running total number of yods should be read upwards, starting from the base in each case.

the 96 corners of the 14 polygons to leave 91 corners, including the two endpoints of the root edge. As will be now proved, if the three other possible orderings of the 14 polygons are considered:

1. triangle→dodecagon→triangle→dodecagon;
2. dodecagon→triangle→dodecagon→triangle;
3. dodecagon→triangle→triangle→dodecagon,

none of them has a yod population that, including the root edge, fits the formula $6N + 4$ for N overlapping TOLs with N greater than 91.

Proof of uniqueness of encoding of CTOL in the (7+5) polygons

The two possible orderings: triangle→dodecagon and dodecagon→triangle create ($2 \times 2 = 4$) possible combinations of the two sets of polygons. Those not considered earlier are:

1) Triangle→dodecagon

The section: triangle→octagon encodes **76** overlapping TOLs (Fig. 11), which is allowable, although uninteresting, being less than the 91 TOLs of CTOL. The section: triangle→decagon encodes the 86-tree, which is disallowed because it only makes sense to look for a number of overlapping TOLs as a *complete* map of all levels of reality. The n -tree is always part of N overlapping TOLs, where $N > n$.

2) Dodecagon→triangle

The section: dodecagon→hexagon encodes **36** overlapping TOLs, which is permissible, but uninteresting, being less than 91. The section: dodecagon→square encodes the **95**-tree, which is disallowed for the reason given above. CTOL is encoded in the section: dodecagon→pentagon.

3) Dodecagon→dodecagon

The two sections: dodecagon→hexagon & dodecagon→octagon encode, respectively, **36** & **76** overlapping TOLs, which are both uninteresting. The section: dodecagon→decagon encodes the 86-tree, which is disallowed.

Although combination (2) is the only one that encodes a number of overlapping TOLs as large as that in CTOL, it also encodes **36** overlapping TOLs in one set of polygons. This is not permitted, because it is only meaningful for a set of polygons encoding as many TOLs as CTOL to have subsets encoding groups of TOLs that are part of CTOL, not separate, overlapping groups. In the 12-polygon section: triangle→pentagon considered earlier, it encodes not only a single number (91) of overlapping TOLs but also the **26**-tree and the **49**-tree, which are both parts of CTOL. It is concluded that, of the four possibilities, only this section is permitted.

We conclude that the encoding of CTOL in this particular set and ordering of 12 polygons is unique. (*En passim*, it is worth noting that the triangle and square uninvolved in this encoding have 44 yods — a very 'Pythagorean' feature in view of the importance of the Tetrad to this philosophy! It is another example of how the Tetrad Principle formulated in Article 1² governs properties of TOL).

In Theosophical terms, the **26**th TOL in CTOL maps the fifth subplane of the fourth (Buddhic) plane, counting in both cases from the lowest plane and subplane of each plane. Malkuth of the **26**th TOL is Tiphareth of the 25th TOL, which is the centre of the seven TOLs mapping the fourth plane, the central one of the seven planes. Malkuth of the **26**th TOL is the pivotal centre of the **49**-tree — its 'half-way point,' so to speak. These **26** TOLs corresponding to the first five polygons denote the region of CTOL that is the counterpart of **26**-dimensional space-time predicted by quantum mechanics for the one-dimensional

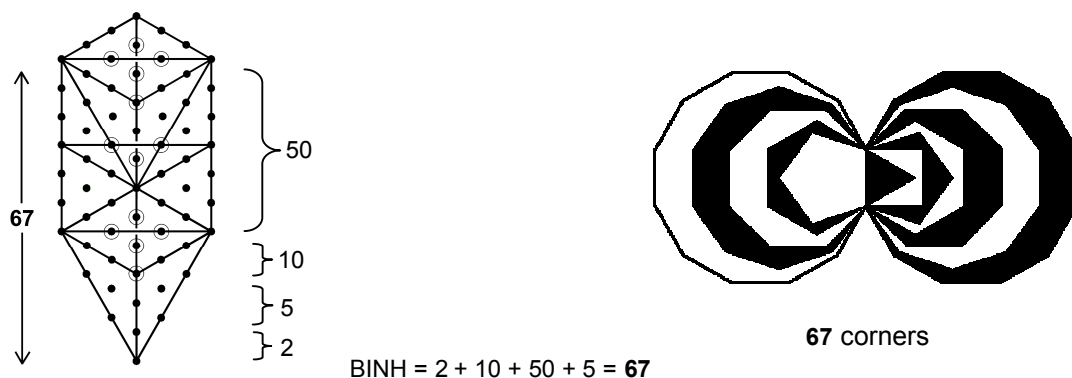
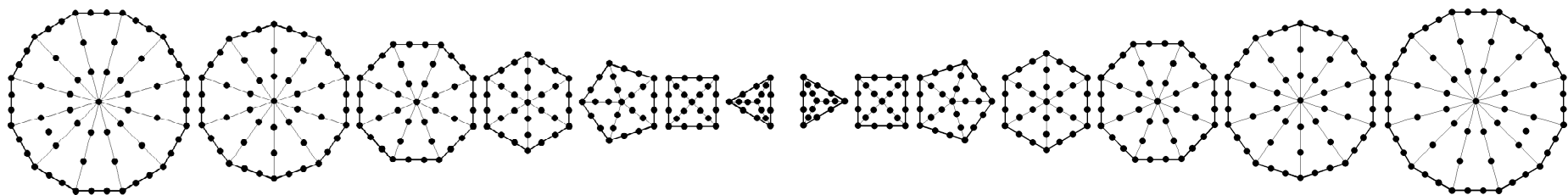
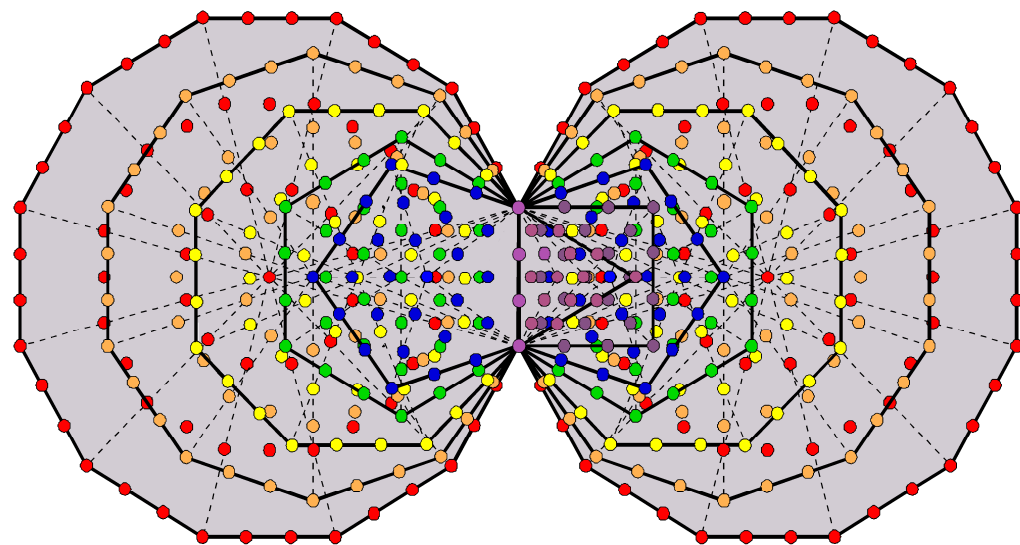
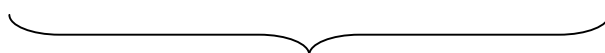
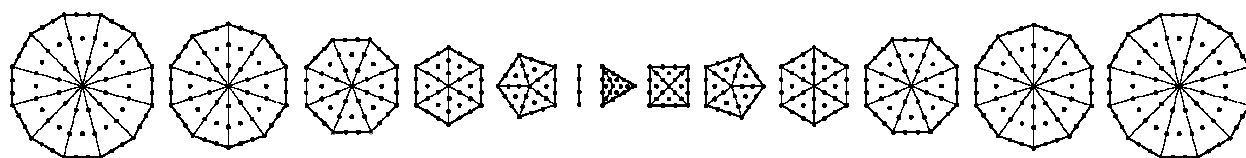
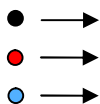
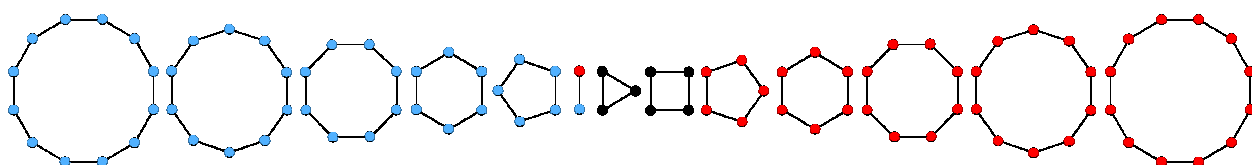
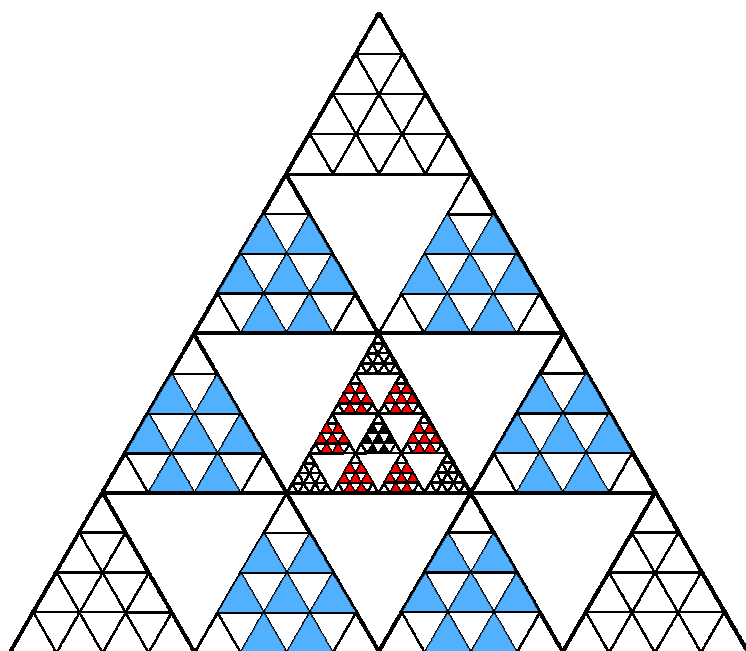


Figure 12. The number value **67** of Binah is the number of yods below this Sephirah in the 1-tree. The letter values of the Hebrew word BINH denote sets of yods. **67** is the number of corners of the (7+5) enfolded polygons belonging to the Inner Tree of Life that separately and together with the root edge have 550 yods and 91 corners when their 89 sectors are tetractyses.





physical plane. Enfolded, they have five vertices. This is an example of a 5:7 pattern that is characteristic of seven-fold, holistic systems. An example is the fact that the seven tone intervals of each of the seven types of musical scales include five whole tone intervals. This pattern is the geometrical manifestation of the fundamental distinction between the five Sephiroth of Construction belonging to the Lower Face of the Tree of Life and the two Sephiroth of Construction (Chesed and Geburah) that are part of its Upper Face.

Enfolded, the (7+5) polygons have **67** corners (Fig. 12). This is the number value of Binah, the Sephirah at the head of the Pillar of Judgement that embodies the archetype governing the basic forms of holistic systems. Remarkably, it is the number of yods below Binah of the 1-tree when its 19 triangles become tetractyses. ELOHIM, the Godname of Binah with number value **50**, prescribes the (7+5) separate polygons because their 89 sectors have **101** corners, where **101** is the **50th** odd integer after 1. They are prescribed by YAHWEH, Godname of Chokmah with number value **26**, because **101** is the **26th** prime number. It is also the number value of *Michael*, the Archangel of Tiphareth. The (7+5) enfolded polygons have **65** corners outside their shared root edge, showing how ADONAI, the Godname of Malkuth with number value **65**, prescribes their outer form. The **87** sectors of the enfolded (7+5) polygons have **76** corners, where **87** is the number value of *Levanah*, the Mundane Chakra of Yesod, and **76** is the number value of YAHWEH ELOHIM, the Godname of Tiphareth (see Article 4 in ref. 1 for how the Godnames of the other Sephiroth prescribe the (7+5) polygons).

What other evidence indicates that the 12 polygons encoding CTOL constitute a holistic system, as indicated by the way in which the number values of the ten Sephiroth in the four Worlds parameterize their properties? Converted into tetractyses, their **87** sectors contain 494 yods (Fig. 13). 247 yods lie on the sides of the **48** tetractys sectors of the seven separate polygons of the Inner TOL. This means that ($2 \times 247 = 494$) yods line the 192 sides of the 96 tetractyses making up both sets of seven polygons. Of these, 110 yods are corners of the latter, leaving 384 hexagonal yods on their sides. Many previous articles have demonstrated that this number is a parameter of holistic systems. For example, it is the number of corners, lines & triangles surrounding the centres of both sets of seven separate polygons. It is also the number of lines and broken lines in the 64 hexagrams of the I Ching table, as well as the number of yods in CTOL up to the top of the seventh TOL, i.e., the number of yods needed to construct from tetractyses the map of the physical plane. The Pythagorean integers 1, 2, 3 & 4 express the number 494 as:

$$494 = \begin{matrix} 1^1 & 2^1 & 3^1 & 4^1 \\ 1^2 & 2^2 & 3^2 & 4^2 \\ 1^3 & 2^3 & 3^3 & 4^3 \\ 1^4 & 2^4 & 3^4 & 4^4 \end{matrix}$$

They also express the 30 yods in the missing triangle and square because

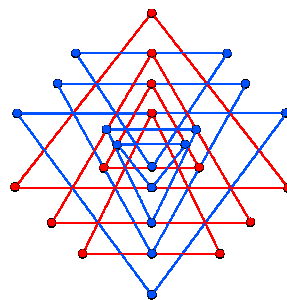
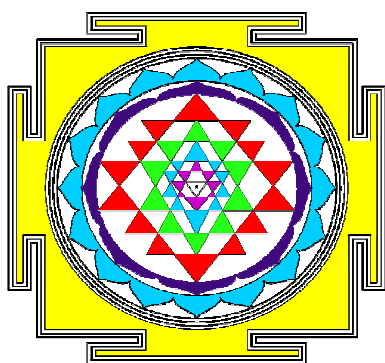
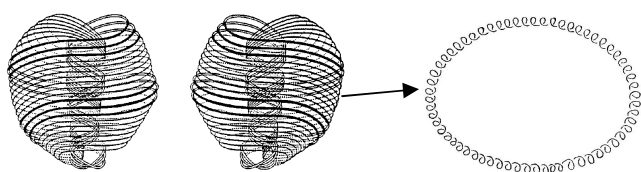
$$30 = 1^2 + 2^2 + 3^2 + 4^2.$$

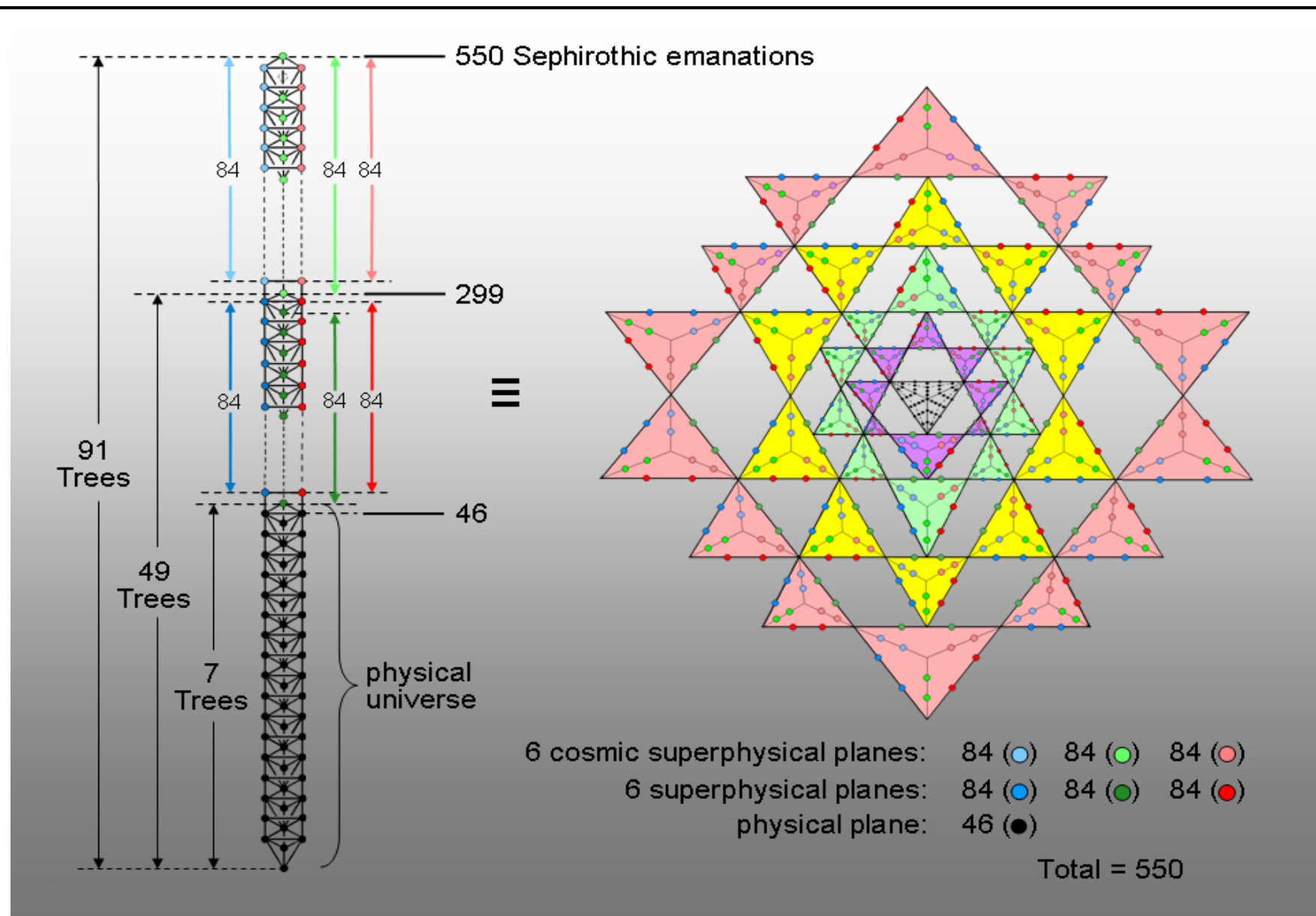
EL ChAI, the Godname of Yesod with number value **49**, prescribes the (7+5) enfolded polygons because they have 490 ($=49 \times 10$) yods outside their root edge. Their **87** sectors have 165 sides, where

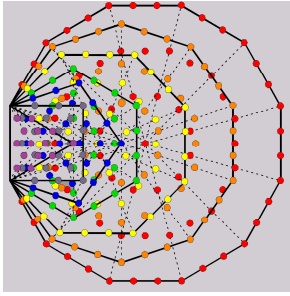
$$165 = 1^2 + 3^2 + 5^2 + 7^2 + 9^2.$$

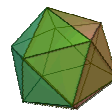
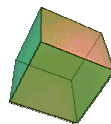
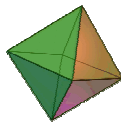
Such simple, mathematical beauty is characteristic of holistic systems.

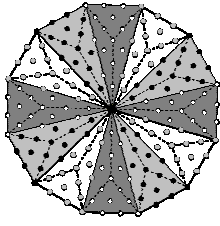
The 295 yods in the seven separate polygons of the Inner TOL symbolize the 295 SLs up to Chesed of the **49th** TOL. The four yods in the separate root edge denote Kether, Chokmah, Binah & Daath of the **49th** TOL. The 251 yods in the five other polygons of the set of 12 symbolize the 251 SLs in CTOL above the top of the **49-tree** (Fig. 14). There are 183 SLs on each side pillar of CTOL and 184 SLs on its central pillar. There are 99 SLs on each side pillar of the **49-tree** and **101** SLs on its central pillar, where **101** is the **26th** prime number and the number value of *Michael*, the Archangel of Tiphareth. Hence, there are ($183 - 99 = 84$) SLs on each side pillar above the **49-tree** and ($184 - 100 = 84$) SLs on the central pillar down to its top. There are **15** SLs on each side pillar of the 7-tree, which is analogous to the **49-tree** because both correspond on their own levels to the Sephirah Malkuth, as well as 17 SLs on the central pillar of the 7-tree. Hence, there are ($99 - 15 = 84$) SLs on each side pillar of the **49-tree** above the 7-tree and ($100 - 16 = 84$) SLs on its central pillar below the top of the **49-tree** down to the top of the 7-tree. This SL, the 47th from the bottom of CTOL, is the **168th** SL on the central pillar, counting from the top of CTOL. **168** is the number value of *Cholem Yesodeth*, the Mundane Chakra of Malkuth. This is remarkable evidence that the 7-tree does, indeed, represent Malkuth. Furthermore, there are ($84 + 84 = 168$) SLs on the side pillar above the **49-tree**, which, too, represents this Sephirah on a greater cosmic level. The 504 SLs down to the top of the 7-tree consist of **168** SLs on each side pillar and **168** SLs on the central pillar. This **168:168:168** division will prove to be highly significant when CTOL is compared in the next section with

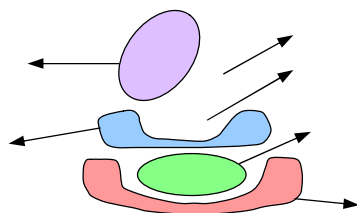
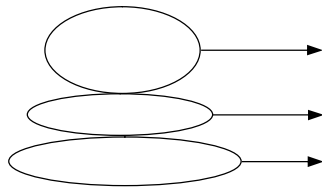


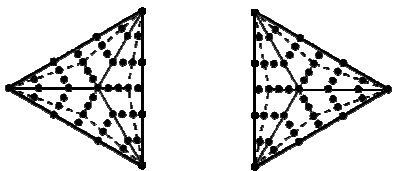
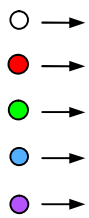
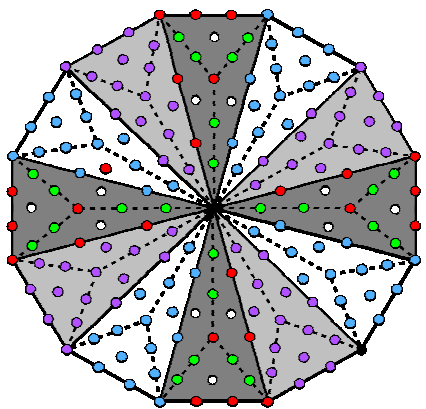












given by Plato in his *Timaeus*. They have 68 corners (30 polyhedral vertices, where $30 = 1^2 + 2^2 + 3^2 + 4^2$), and 180 sides (60 polyhedral edges). The holistic parameter 180, which was earlier encountered as the 180 sectors of the five Platonic solids, reappears in the first four Platonic solids as the number of sides of their 120 triangular sectors.

E_8 has eight simple (or zero) roots and 240 non-zero roots. Comparing this with the **248** corners & sides in the 38 faces of the first four Platonic solids, Table 5 indicates that the number 8 appears three times, namely, as the eight corners of the 12 sectors in the tetrahedron, as the eight corners at the centres of the faces of the octahedron and as the eight corners of the cube. Rather than try to answer the question of which polyhedron embodies the corners corresponding to the simple roots, let us just note that the 120 sectors in the 38 faces have 60 corners and 180 sides, i.e., 240 corners & sides. They correspond to the 240 non-zero roots of E_8 . The 180 sides comprise 12 sides that belong either to the tetrahedron, the octahedron or the cube and **168** other sides, where **168** is the number value of *Cholem Yesodeth*, the Mundane Chakra of Malkuth. The latter comprise 78 sides of the 60 sectors of the first three solids and 90 sides of the 60 sectors of the icosahedron. This is remarkable because it reproduces the number values of *Cholem* and *Yesodeth*:

$$168 = \begin{array}{c} \text{יְסוּדוֹת} \quad \text{חֵלֶם} \\ \text{T U D U S Y} \quad \text{M L Ch} \\ \underbrace{4 \leftarrow 400 \quad 6 \quad 4 \quad 6 \quad 60 \quad 10}_{90} \quad \underbrace{40 \quad 30 \quad 8}_{78} \end{array}$$

The gematria number value of *Cholem Yesodeth*. The number value 400 of T (tau) is contracted to 4.

However, it is unsurprising, as this division *always* manifests in holistic systems, as has been demonstrated in many previous articles. The counterpart of the 240 non-zero roots of E_8 in the 38 faces of the first four Platonic solids are the 60 corners, the 12 unspecified sides and the **168** other sides, i.e., **72** corners & sides and **168** sides, totalling 240 corners & sides. The former correspond to the **72** roots of E_6 , the rank-6 exceptional subgroup of E_8 and the latter correspond to the **168** roots of E_8 that are not also roots of E_6 .

- 4) When the 60 sectors of the 12 pentagonal faces of the dodecahedron are turned into tetractyses and the 90 sectors of the 30 internal triangles formed by its centre and edges are turned into tetractyses, 550 hexagonal yods are generated.⁸ Plato regarded this regular solid as representing the celestial sphere because it resembled the perfect shape of a sphere more than any other one. We now see that not only do the five Platonic solids represent CTOL but so, too, does the fifth one by itself! Each hexagonal yod in the 150 tetractyses needed to construct the dodecahedron symbolizes one of its 550 SLs. The holistic parameter 550 embodied in all five Platonic solid manifests in the last one as well.

6. The disdyakis triacontahedron represents CTOL

The faces of the Platonic solids are regular polygons with the same shape and size. The 13 Archimedean solids have faces with the shapes of two or more regular polygons. Interchanging vertices and faces generates their duals — the 13 Catalan solids. The Catalan solid with the most vertices is called the disdyakis triacontahedron. Article 23⁹ proved that this semi-regular polygon is the outer form of the polyhedral version of the Tree of Life and all its equivalent sacred geometries (its

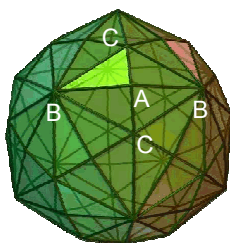


Figure 24. The disdyakis triacontahedron and its three types of vertices.

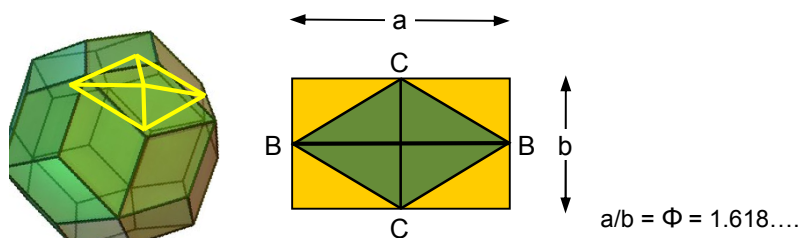
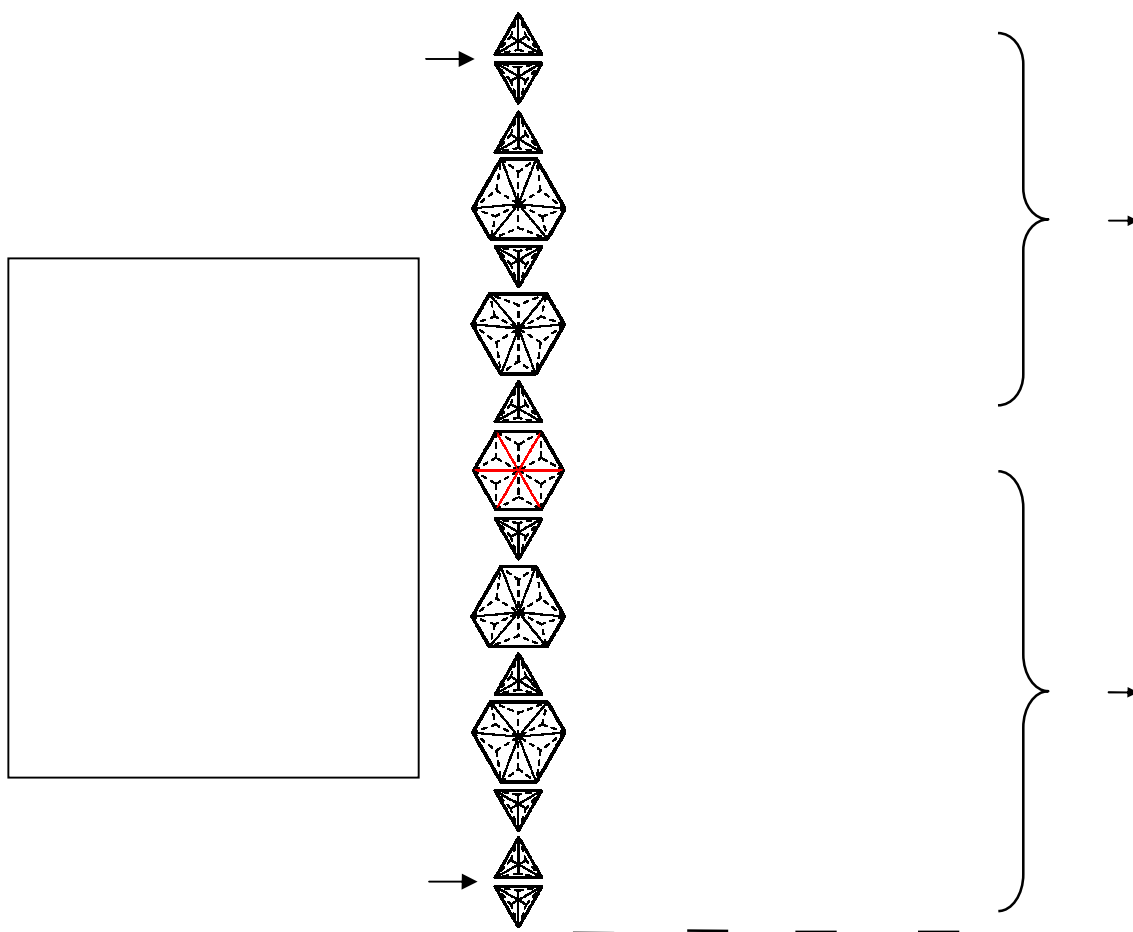
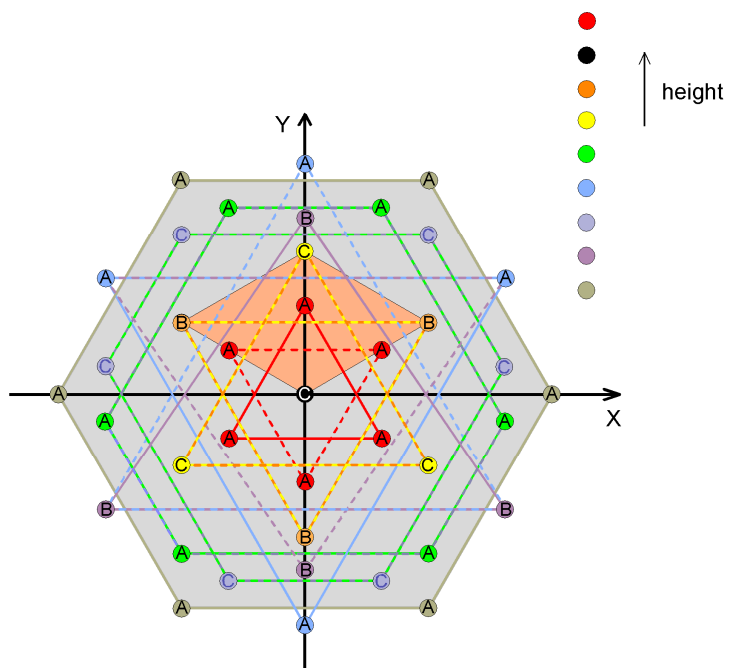


Figure 25. The 30 golden rhombic faces of the rhombic triacontahedron underlying the disdyakis triacontahedron are the bases of 30 pyramids (outlined in yellow) with 120 faces.

inner form — the polyhedral counterpart of the polygonal Inner Tree of Life — is a polyhedron with 74 vertices, **216** edges & 144 faces). The disdyakis triacontahedron (Fig. 24) has **62** vertices, 180 edges and 120 triangular faces, that is, 362 geometrical elements make up its faces. Including its centre, there are **363** elements, where **363** is the number value of SHADDAL EL CHAI, the complete Godname



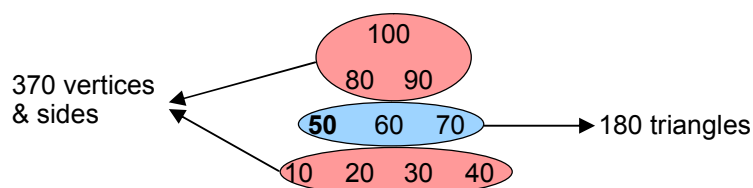
of Yesod. The vertices are of three kinds: the 12 B vertices are vertices of an icosahedron, the 20 C vertices are vertices of a dodecahedron and the 30 A vertices are vertices of rhombic pyramids stuck on the 30 faces of a rhombic triacontahedron (Fig. 25). They are in fact golden rhombic faces because the ratio of their two diagonals (the edges of the underlying icosahedron and dodecahedron) is the Golden Ratio Φ . This means that the bases of all the diamond-shaped facets of the disdyakis triacontahedron have this aesthetically pleasing proportion used for centuries by artists and architects.

Φ is present in this polyhedron in a more subtle way. Imagine a straight line passing through two opposite C vertices. It will be referred to as the C-C axis. As there are 20 C vertices, there are ten different C-C axes. For present purposes, however, only one need be considered. The 60 vertices (30 A, 12 B & 18 C) surrounding a C axis are arranged in **15** sheets or layers. They are the corners of seven polygons either above or below the central plane, which have six vertices arranged at the corners of a hexagon. Table 6 lists the rectangular coordinates of all **62** vertices. Each is a function of Φ , the distances between adjacent polygons being an integer power of Φ .

Figure 26 displays the positions of polyhedral vertices plotted in the XY plane with the C axis along the Z axis. It shows that each of the **15** polygons has corners that are polyhedral vertices of the same type. This means that none of their 60 sides are edges of the disdyakis triacontahedron. Moreover, if the sectors of the polygons are Type A triangles, i.e., themselves divided into three triangles, only the centre of the central hexagon and the internal sides of its six sectors (shown red in Fig. 27) are shared with the 180 ordinary triangles inside the polyhedron formed by its centre and its 180 edges. The centres of the 14 polygons above and below the central polygon, the edges of their sectors and the sides of the three triangles in each sector of a polygon are unshared with the polyhedron, as are the 24 internal sides of the 18 triangles in the sectors of the central Type B hexagon. The two opposite C vertices on the Z axis are unshared with the polygons. Including these, the number of unshared geometrical elements is shown below:

	vertices	sides	triangles
	2		
	14	$5 \times 60 = 300$	$60 \times 3 = 180$
	60	-6 (shared)	
Total =	76	+ 294	+ 180 = 550.

There are 550 such elements, shown in detail in Fig. 27. They consist of **76** vertices, 294 sides & 180 triangles, i.e., **474** sides & triangles, where **474** is the number value of Daath ("knowledge") and **76** is the number value of YAHWEH ELOHIM, the Godname of Tiphareth. There are 256 vertices & triangles, where $256 = 4^4$, showing how the Tetrad expresses this number. Remarkably, the 180 triangles and the 370 vertices & sides correspond to the 180 triangles and the 370 vertices & sides making up the **50** faces of the five Platonic solids (see Table 1). Indeed, the *same* 180:370 division appears in the tetractys representation of the number 550 discussed in Section 5:



The 548 unshared geometrical elements other than the two opposite C vertices are the counterpart of the 548 SLs between the apex and nadir of CTOL, the C vertices playing the role of the latter. *The disdyakis triacontahedron is the polyhedral representation of CTOL, the unshared geometrical elements of its 15 polygons corresponding to SLs.*

The central hexagon has $(6 \times 3 = 18)$ unshared triangles with six unshared corners and $(6 \times 4 = 24)$ unshared sides surrounding its centre. The 14 polygons above and below the central hexagon have 14 unshared centres and $(60 - 6 = 54)$ unshared corners of $(180 - 18 = 162)$ unshared triangles with $(294 - 24 = 270)$ unshared sides, i.e., 500 $(= 50 \times 10)$ geometrical elements unshared with the internal triangles of the disdyakis triacontahedron. This shows how ELOHIM, the Godname of Binah with number value **50**, prescribes the 14 polygons. Each set of seven polygons has 250 unshared elements. Including the two C vertices, 251 elements are either above or below the central hexagon, which has $(6 \times 8 = 48)$ unshared elements (one corner, four sides & three triangles per sector). **48** is the number value of *Kokab*, the Mundane Chakra of Hod. Hence, the eight polygons making up the lower half of the disdyakis triacontahedron have $(251 + 48 = 299)$ unshared geometrical elements, 251 unshared elements being above the central hexagon.

Δ				
▽				
Δ				
○				
▽				
○				
Δ				
○				

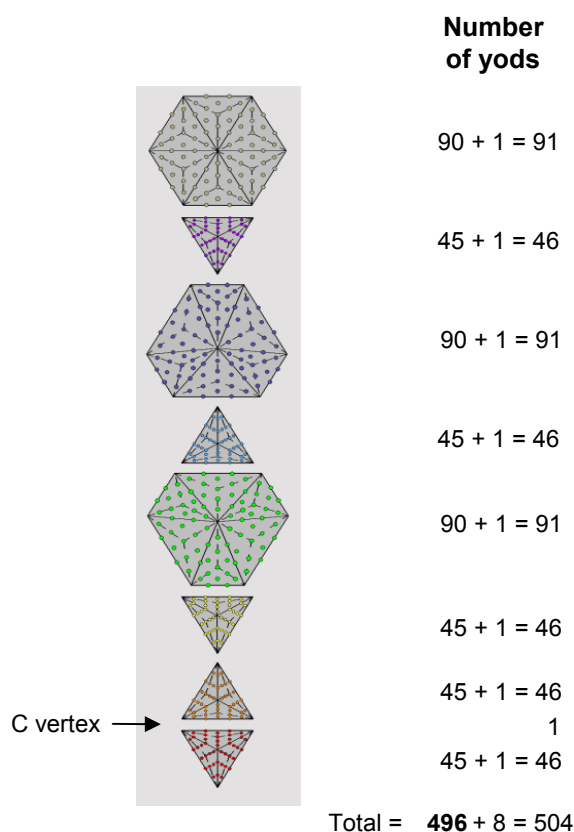


Figure 28. The 504 yods in the lowest eight Type B polygons (C vertex included) comprise **496** yods that surround their eight centres.

them.

Including the C vertex, there are 504 yods in half the polyhedron (Table 7 & Fig. 28). There are **496** yods other than centres of its eight polygons. This is the number value of Malkuth, the last Sephirah of the Tree of Life denoting its physical form. The very half of the polyhedron whose 299 geometrical elements are analogous to the 299 SLs of the **49**-tree mapping the cosmic physical plane embodies the number value of the Kabbalistic name of the Sephirah that is associated with this section of CTOL! Such an amazing property refutes the suggestion that it might be merely coincidence that there are 550 geometrical elements in the **15** Type B polygons and the two opposite C vertices, quite apart, of course, from the equally remarkable 299:251 division in elements that compose the polygons in one half of the polyhedron and its remainder. Another piece of evidence that discounts the possibility of coincidence is the fact that 66 corners of tetractyses surround the centres of the eight polygons in half the polyhedron. As 66 is the **65**th integer after 1, this property is aptly prescribed by ADONAI, the Godname of *Malkuth* with number value **65**.

According to Table 7, including a C vertex, the number of yods in the seven polygons either above or below the central hexagon with 91 yods is 413. Including the two C vertices, the number of yods in the **15** polygons = $2 \times 413 + 91 = 917$. 916 yods surround the centre of the disdyakis triacontahedron. The number of yods on the central Pillar of Equilibrium of n overlapping TOLs constructed from tetractyses is given by

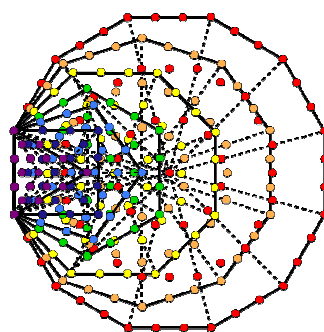
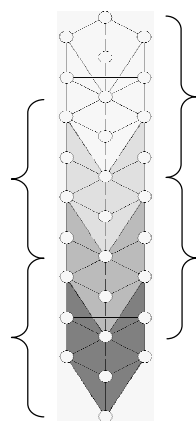
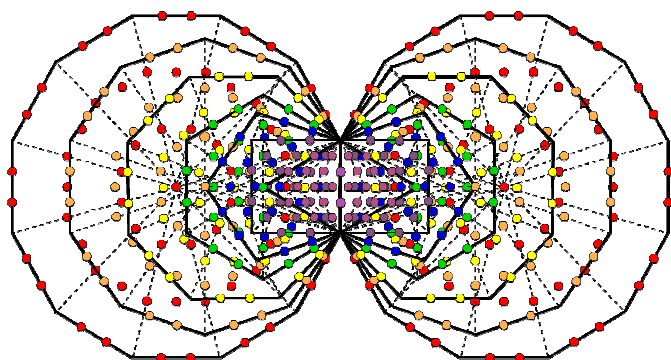
$$N(n) = 10n + 6.^{10}$$

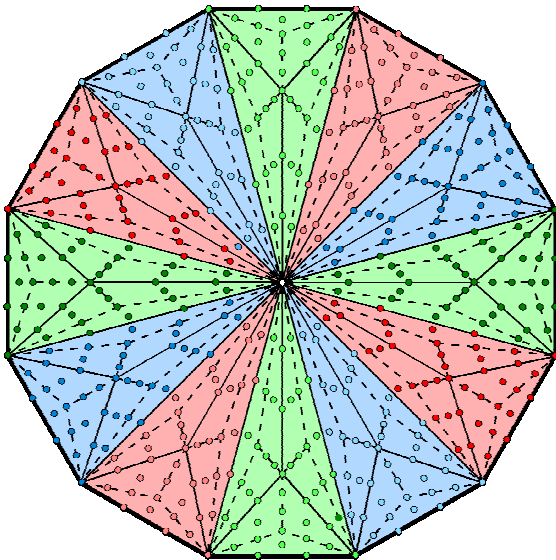
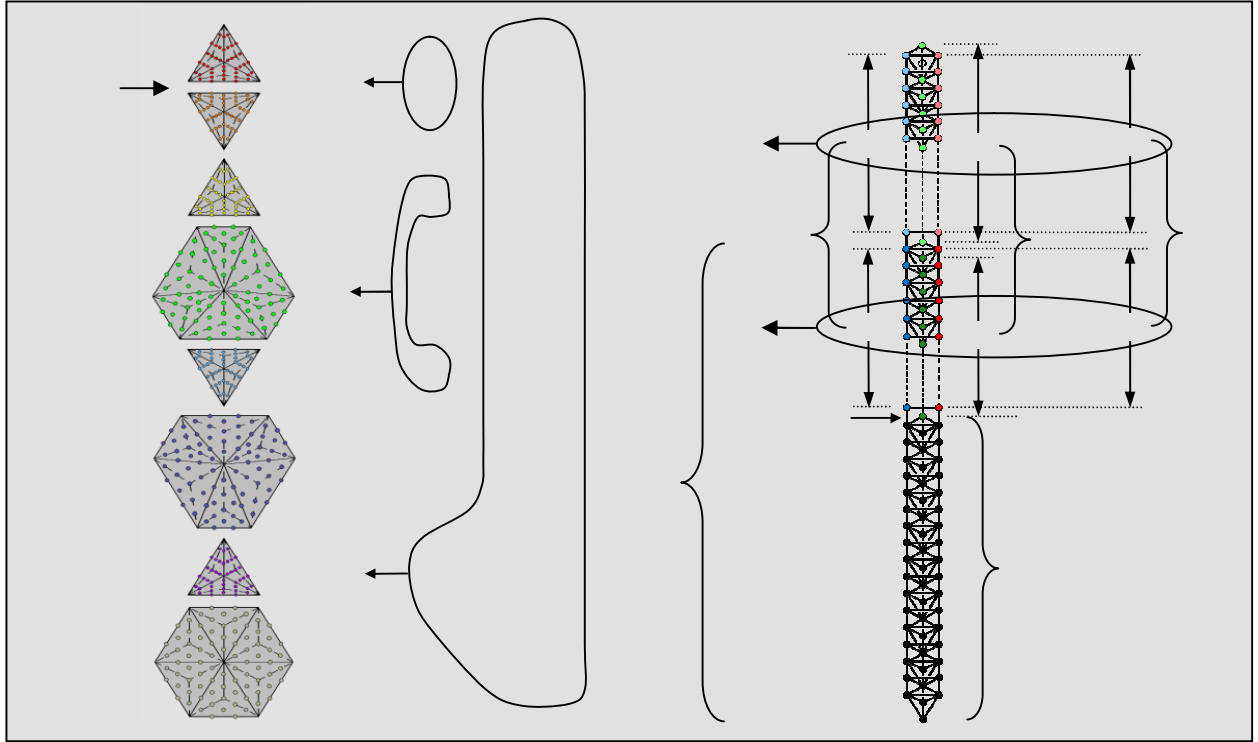
Hence, $N(91) = 916$. The number of yods surrounding the centre of the disdyakis triacontahedron is exactly equal to the number of yods that lie on the central pillar of CTOL when its 1096 triangles are tetractyses! Here is further, spectacular evidence that this polyhedron is the polyhedral counterpart of CTOL. The geometrical elements composing the **15** polygons perpendicular to a C-C axis correspond to SLs between the apex and nadir of CTOL, whilst their yods correspond to yods lying on its central pillar.

The number of yods on the central Pillar of Equilibrium of the n -tree (the lowest n TOLs in CTOL) is given by

$$\check{N}(n) = 10n + 10.^{11}$$

Hence, $\check{N}(49) = 500$. There are four more yods up to, but not including, Daath of the **50**th TOL. The 504 yods in the eight polygons (including the C vertex) correspond to the 504 yods on the central pillar of CTOL up to this SL. Its significance is that it is the next lower SL after Binah of the **50**th TOL, where **50** is





the inner form of four overlapping TOLs = $4 \times 229 = 916$. This is the number of yods lying on the Pillar of Equilibrium of CTOL. Different representations of the same holistic system are always parameterized by the same set of numbers.

The counterpart in the Sri Yantra of the 504 SLs in CTOL down to the top of the 7-tree mapping the physical universe are the 504 hexagonal yods lying on the sides of tetractyses in the 42 triangles. They consist of 252 hexagonal yods on the outer sides of these triangles (three sets of 84) and 252 hexagonal yods (three sets of 84) inside them. They symbolized the 84 SLs in each of the three pillars of CTOL down to the top of the **49**-tree and the 84 SLs in each of the three pillars below the top of the **49**-tree down to the top of the 7-tree. What is the counterpart of this $3 \times 84 : 3 \times 84$ pattern in the 504 yods (including

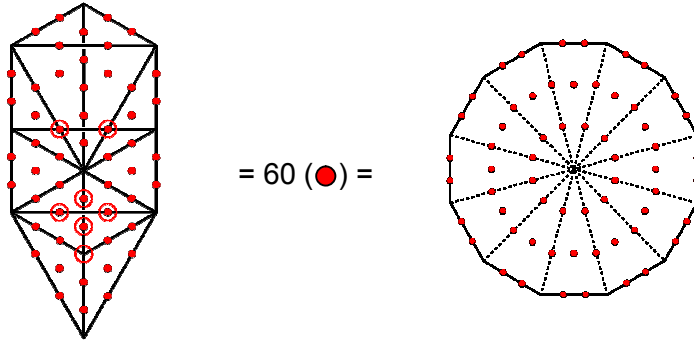


Figure 34. The Type A dodecagon has as many hexagonal yods as the Tree of Life because this polygon is its polygonal counterpart.

the upper C vertex) in the eight polygons in the upper half of the disdyakis triacontahedron? Figure 32 shows that 84 yods other than corners surround the centre of each of the three six-sided polygons. 84 yods other than corners surround the centres of two triangles, 84 yods other than corners surround the centres of two more triangles, leaving 84 yods made up of the C vertex, the yods in the last triangle and the corners & centres of all eight polygons. That particular triangle has been chosen only for illustration, for it is not obvious which triangle should be included with the corners and centres. Whichever is the correct one is irrelevant to what is demonstrated here, namely, that the 504 yods in the **15** polygons (including the C vertex) *naturally and simply* divide into six sets of 84 yods, as should be expected if the disdyakis triacontahedron embodies a map of all superphysical levels of reality that is analogous to CTOL.

The same pattern exists in the distribution of 504 yods that surround the centre of a Type C dodecagon (Fig. 33). Pairs of opposite sectors contribute 84 yods. The 84 light and 84 dark yods symbolize, respectively, the 84 SLs on the Pillar of Mercy above the **49**-tree and between the 7-tree and the **49**-tree. The light and dark green yods denote the corresponding SLs on the Pillar of Equilibrium and the light and dark blue yods denote the corresponding SLs on the Pillar of Judgement. As the last regular polygon of the Inner TOL, the dodecagon is the *single* polygonal counterpart of the Tree of Life. This is demonstrated by the fact that the 60 hexagonal yods in a Type A dodecagon are analogous to the 60 hexagonal yods in

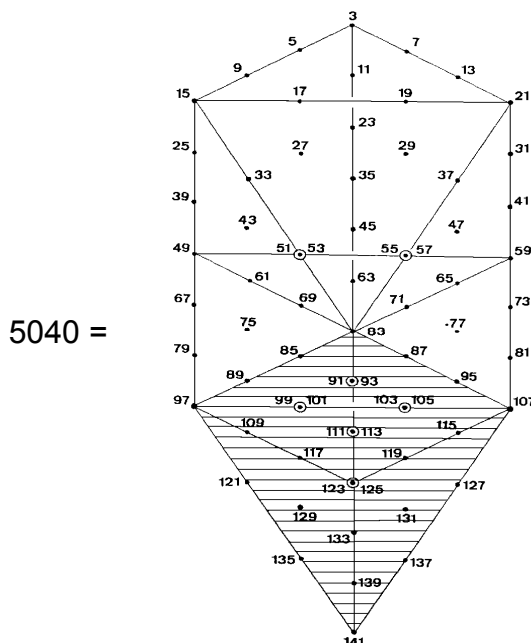


Figure 35. The sum of the 40 odd integers after 1 that can be assigned to the 40 yods in the tree of Life above the Lower Face (shown shaded) is 1680. The sum of the next 30 odd integers assigned to the 30 yods in the Lower Face is 3360 = 2×1680 . Their sum is 5040.

the Tree of Life itself when its 16 triangles are tetractyses (Fig. 34). Only this polygon can have such a number of hexagonal yods. Its Tree of Life character is the reason why **168** yods are needed to turn it into a Type B dodecagon and why 504 yods are needed to convert it to a Type C dodecagon. The former correspond to the **168** SLs on the central pillar of CTOL down to the top of the 7-tree mapping the physical universe. The extra 2×168 yods correspond to the **168** SLs on each side pillar (this is an alternative to the representation in Fig. 33 of the 504 SLs).

As we have seen, the **168:168:168** division of SLs distributed on the three pillars of CTOL above the 7-tree is characteristic of holistic systems. It was encountered in Article 43¹³ in the discussion of the {3,7} tessellation of the 3-torus mapping the **168** automorphisms of the Klein quartic as the **168** hexagonal yods on the edges of its 56 triangles when they are tetractyses and as the 336 hexagonal yods added, generating 504 hexagonal yods, when the sectors of these triangles are tetractyses. The geometry of the tessellated 3-torus was shown to be analogous to the Tree of Life, embodying its parameters.

The number 504 and its **168:336** division is embodied arithmetically in the Tree of Life for the following reason: assigning the 70 odd integers after 1 to its 70 yods generates the number 5040 because

$$71^2 - 1 = 3 + 5 + 7 + \dots + 141 = 5040.$$

This is the number of yods in 504 tetractyses. There are 40 yods above the Lower Face. Assigning the first 40 odd integers after 1 to them generates the number 1680 because

$$41^2 - 1 = 3 + 5 + 7 + \dots + 81 = 1680.$$

This is the number of yods in **168** tetractyses. This means that the 30 integers 83-141 assigned to the 30 yods in the Lower Face add up to 3360, which is the number of yods in 2×168 tetractyses. The distinction between the Lower Face and the rest of the Tree of Life creates in an arithmetic way the **168:2×168** division characteristic of holistic systems. It is remarkable that this purely geometrical distinction divides the 70 yods into precisely the sets of 40 and 30 yods that generate this division when the odd integers after 1 are assigned to them. It is an example of the beautiful harmony between number and geometry displayed by sacred geometries. It manifests in the three uppermost whorls of the UPA shown in Fig. 15, which C.W. Leadbeater described as thicker than the lower seven ones, each whorl being a helix with 1680 circular turns. As the microscopic manifestation in space-time of the Tree of Life, the three whorls correspond to the Supernal Triad of Kether, Chokmah & Binah, whilst the seven other whorls correspond to the seven Sephiroth of Construction.

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- ¹ Phillips, Stephen M. Article 4: "The Godnames prescribe the inner Tree of Life," <http://www.smphillips.8m.com/Article04.pdf>, p. 6.
- ² Phillips, Stephen M. Article 1: "The Pythagorean nature of superstring and bosonic string theories," <http://www.smphillips.8m.com/Article01.pdf>, p. 4.
- ³ Besant, A. & Leadbeater, C.W.: "Occult Chemistry," Theosophical Publishing House, Adyar, Chennai, India, 1951, p. 23.
- ⁴ Phillips, Stephen M. Article 35: "The Tree of Life nature of the Sri Yantra and some of its scientific meanings," <http://www.smphillips.8m.com/Article35.pdf>.
- ⁵ See ref. 4 for how other number values of the ten Sephiroth in the four Worlds are present in the Sri Yantra.
- ⁶ Proof: Let p = the number of sides of each face (or the number of vertices of each face) and q = the number of faces meeting at each vertex (or the number of edges meeting at each vertex). Then, for a regular polyhedron with C vertices, E edges and F faces, $pF = 2E = qC$. Substituting these in Euler's formula for a polyhedron:

$$C - E + F = 2,$$

$$2E/q - E + 2E/p = 2,$$

so that

$$1/q + 1/p = \frac{1}{2} + 1/E.$$

Since E is positive,

$$1/q + 1/p > \frac{1}{2}.$$

Allowed values of p and q are $p = 3, q = 3$ (tetrahedron), $p = 4, q = 3$ (cube), $p = 3, q = 4$ (octahedron), p

= 5, q = 3 (dodecahedron) & p = 3, q = 5 (icosahedron).

⁷ Phillips, Stephen M. Article 46: "How sacred geometries encode the 64 codons of mRNA and the 64 anticodons of tRNA," <http://www.smphillips.com/Article46.pdf>, Fig. 38b.

⁸ See Table 1 in Article 3 at <http://smphillips.8m.com/html/articles.html>.

⁹ Phillips, Stephen M. Article 23: "The polyhedral Tree of Life," <http://www.smphillips.8m.com/Article23.pdf>.

¹⁰ Proof: n overlapping Trees of Life have (n+1) Faces. Each of the lowest n Faces has 10 yods on the Pillar of Equilibrium when all triangles are tetractyses and the (n+1)th Face has 6 yods. Number of yods on the central pillar of n overlapping Trees of Life $\equiv \check{N}(n) = 10n + 6$.

¹¹ Proof: the n-tree has (n+1) Faces, each with 10 yods on the central Pillar of Equilibrium. Number of yods on the central pillar of the n-tree = $10(n+1) = 10n + 10$.

¹² Proof: The seven enfolded polygons have 42 sides. Their 47 sectors have 46 internal sides. When each polygon is Type B, their 47 sectors add (47×3=141) sides. Number of sides of seven enfolded Type B polygons = 42 + 46 + 141 = 229.

¹³ Phillips, Stephen M. Article 43: "The Tree of Life nature of the {3,7} tessellation of the 168 automorphisms of the Klein quartic on the 3-torus," <http://www.smphillips.8m.com/Article43.pdf>, Table 3.